Effect of Proportion of Missing Data on Application of Data Imputation in PMS

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7	
8	Abstract
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10	Missing data are commonly found in pavement condition/performance databases. A common
11	practice today is to apply statistical imputation methods to replace the missing data with
12	imputed values. It is thus important for pavement management decision makers to know the
13	uncertainty and errors involved in the use of datasets with imputed values in their analysis. An
14	equally important information of practical significance is the maximum allowable proportion
15	of missing data (i.e. level of data missingness in the pavement condition/performance records)
16	that will still produce results with acceptable magnitude of error or risk when using imputed
17	data. This paper proposes a procedure for determining such useful information. A numerical
18	example analyzing pavement roughness data is presented to demonstrate the procedure through
19	evaluating the error and reliability characteristics of imputed data. The roughness data of three
20	road sections were obtained from the LTPP database. From these data records, datasets with
21	different proportions of missing data were randomly generated to study the effect of level of
22	data missingness. The analysis shows that the errors of imputed data increased with the level
23	of data missingness, and their magnitudes are significantly affected by the effect of pavement
24	rehabilitation. On the application of data imputation in PMS, the study suggests that at 95%
25	confidence level, 25% of missing data appears to be a reasonable allowable maximum limit for
26	analyzing pavement roughness time series data not involving rehabilitation within the analysis
27	period. When pavement rehabilitation occurs within the analysis period, the maximum
28	proportion of imputed data should be limited to 15%.
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Effect of Proportion of Missing Data on Application of Data Imputation in PMS

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40 INTRODUCTION

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Engineering analysis and decision making in a pavement management system (PMS) are datadriven processes heavily dependent on the quality and accuracy of the data records. Unfortunately, in practice, the data records in most pavement management systems contain missing data (1-3). Therefore, missing-data management is an important element in the engineering analysis and decision making of a pavement management system. According to an NCHRP Synthesis Report (4), 61% of the pavement agencies in USA included in a survey used software routine to check for missing data.

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Since pavement condition and performance data are time-specific information, re-collection of 50 missing past records through field survey is not possible nor meaningful. Under this situation, 51 52 the PMS engineer has the option to discard the records with missing data and proceed with the remaining records. This is not always desirable as it means making engineering analysis with 53 54 a reduced data space, and ignoring some recorded data which could have important 55 implications to pavement maintenance or traffic operations. A procedure which is increasingly being adopted today is to apply suitable data imputation techniques to fill up the incomplete 56 records with imputed values and perform engineering analysis without discarding those records 57 (4-6).58

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60 In the application of data imputation methods to manage missing data records in PMS, one must be aware that the techniques are statistical in nature and uncertainties are involved in the 61 62 imputed data values. Knowing the likely magnitudes of the errors involved and the reliability of the dataset containing imputed data would allow the engineers to make informed decisions 63 whether to discard the incomplete data records or to proceed with the full set of records made 64 65 complete with imputed data. Therefore, a relevant issue is to determine the upper limit of the proportion of missing data at which filling up the incomplete data records with imputed data 66 would still provide an accurate representation of the pavement condition. This is the focus of 67 68 the present research. Using pavement roughness data from the Long-Term Pavement Performance Program (LTPP) database, this study examines how different proportions of 69 missing data would affect the accuracy and reliability of imputed datasets. 70

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72 SIGNIFICANCE OF STUDY

73 The theory and principle of statistical quality assurance, in regard to the imputation of missing data, are well developed and has been applied by researchers and practitioners in a number of 74 field of studies, notably in the disciplines of medical studies and social sciences (7-10). The 75 issue of the upper limit threshold for the application of data imputation procedures has also 76 been addressed by researchers in those disciplines. For instance, Schafer (11) suggested using 77 78 statistical data imputation approaches in medical research only when not more than 5 percent 79 data is missing. On the other hand, in dealing with missing data in public health studies, Bennett 80 (12) recommended 20 percent missing data as the maximum threshold for the application of data imputation procedures. However, in their studies of palliative and end-of-life care, Preston 81 et al. (13) recommended that high rates of attrition or missing data should not be seen as 82 83 indicative of poor design and that it is more important to design a clear statistical analysis plan to account for missing data and attrition. 84

86 Little and Rubin (14) introduced the concept of missingness to highlight the importance of the influence of the pattern of missing data on (i) the overall bias introduced, and (ii) the proportion 87 88 of missing data that is too high for creating a reasonable a "complete" dataset. For example, in the case that a very high proportion of data (much higher than 20%) were "missing 89 completely at random", one could still re-create the dataset with imputed data and capture the 90 91 essential characteristics of the original data records. Schlomer et al. (15) concurred that the pattern of data missingness is a major factor of consideration, but stressed that in determining 92 whether a certain amount of missingness is problematic, one must first determine if the 93 94 resultant imputed dataset has adequate statistical power to detect the effects of interest.

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96 It is clear from past research in various disciplines on the applications of data imputation in missing-data management that no simple guidelines can be set for the maximum allowable 97 proportion of missing data across the board covering all fields of studies. The effect of the 98 99 proportion of missing data on the quality of analysis using imputed datasets depends on the nature and characteristics of the data, as well as the pattern of missing data; and statistical 100 analyses must be performed to provide a fuller assessment of the effect so that the decision 101 maker can make an informed decision on how to manage the missing data and the way the data 102 should be used. 103

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105 To the knowledge of the authors, in the field of pavement management studies, in regard to the use of imputed datasets in pavement management analysis, their impact on data quality and 106 107 reliability, and the possible bias introduced to the analysis have not been studied. No guidelines are available concerning the data management procedure necessary to deal with datasets 108 containing different extents of missing data. As missing data are commonly encountered in 109 110 pavement management data records, the availability of the aforementioned information related to the use of imputed data would have high practical significance. This paper attempts to 111 provide some information to partially bridge this knowledge gap by analyzing the effect of 112 missing data in pavement roughness records. 113

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115 APPROACH AND METHODOLOGY OF STUDY

116 Scope of Study

The common types of pavement condition and performance data that are regularly collected in a typical pavement management system include pavement distress data (such as cracks, ruts, potholes, depressions, etc), roughness, friction, and structural condition data derived from nondestructive falling-weight deflectometer testing. Since the nature and characteristics of each of these types of data are quite different from one another, it is likely that they will be affected by missing data differently. It would require a major research effort to examine the effects of missing data on all types of pavement condition/performance data.

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The scope of the present study is limited to the analysis of the effect of missing data in 125 pavement roughness records. The framework and concept of the proposed analysis will be 126 described in this section, followed by a demonstration using an example involving actual 127 pavement roughness data records. Through the analysis of the numerical example, it is 128 demonstrated that useful informative insight can be gained into the quality of imputed data 129 obtained, the magnitude of errors involved as the proportion of missing data increases, and the 130 statistical reliability implications of the imputed dataset as a function of the proportion of 131 132 missing data.

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134 Framework of Analysis

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For the purpose of studying the error and reliability characteristics of imputed data, complete records of pavement roughness data without any missing data were first obtained. These full records of actual measured roughness data will serve as the base reference for assessing the quality and reliability characteristics of datasets containing imputed data. The datasets containing missing data are artificially generated randomly from the original complete data records for the purpose of studying the effects of introducing imputed data.

- 142
- 143 The proposed analysis consists of the following steps:
- (1) Selection of complete data records -- The Federal Highway Administration's (FHWA)
 Long-Term Pavement Performance Program (LTPP) database (*16*) offers a convenient
 source for the selection of pavement roughness data records for the present study. The
 roughness data are reported in terms of the International Roughness Index (IRI).
- (2) Creation of datasets having different levels of data missingness and different patterns of 148 missingness -- To study the effect of the level of data missingness (i.e. proportion of 149 missing data), at least six equally spaced levels of data missingness were first identified. 150 151 Next, for each specified level of data missingness, a random process was employed to generate a dataset containing the correct number (say *n* number) of missing data by 152 randomly deleting n data points from the original complete data records. This random 153 deletion process is repeated another 9 times so as to produce a total of 10 randomly 154 generated datasets, each with a different patterns of missingness, for each of the 6 or 155 more levels of data missingness studied. 156
- (3) Computation of imputed values for each dataset containing missing data -- For each of 157 the datasets containing missing data earlier generated in Step 2, apply a suitable data 158 imputation method to compute a data value for each of the missing data. At the end of 159 this step, all the datasets with missing data generated in Step 2 would be transformed into 160 datasets containing imputed data values. That is, there would be 10 datasets containing 161 imputed data for each level of data missingness. The technique of Multiple Imputation 162 (MI) was adopted for computing imputed data in this study. The imputed value for each 163 missing data in each of the 10 generated datasets is obtained as the mean value of 10 164 imputation runs. The concept and procedure of computation of the MI technique is 165 166 explained in the next section.
- (4) Performing of error and reliability analysis Using the original complete data records as
 the base reference, the errors of the imputed data can be computed and analyzed. The
 variation of the errors with the level of data missingness can be examined. The statistical
 reliability of the imputed datasets at different levels of data missingness can also be
 established by means of hypothesis testing.
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173 Multiple Imputation (MI) Technique for Data Imputation

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The most widely used method today in performing data imputation for missing data is the Multiple Imputation technique first introduced by Rubin (17). This method is known to produce unbiased imputed data and parameter estimates (14, 17, 18). The authors have demonstrated in their earlier work (19) that the Multiple Imputation method out-performed the conventional methods (such as the deletion method, and the substitution methods using mean, interpolation, or regression) in handling missing pavement condition/performance data, and provides an effective approach to impute missing data required in a pavement managementsystem.

The process of Multiple Imputation consists of three main phases: imputation, analysis and 183 polling phase. In the imputation phase, the available measured data are used to estimate 184 distribution parameters, which are then used to estimate the missing data values. In the analysis 185 186 phase, each imputed value is analyzed together with the corresponding available ones using statistical procedure to produce a new imputed value. This iterative process continues until the 187 imputed value changes very little from one iteration to the next. By repeating this procedure, 188 multiple imputations of the missing values are generated. Finally, on the pooling phase, the 189 integration of the multiple imputation results into a single set of result to produce overall 190 estimates and standard errors that reflect missing-data uncertainty. These combined standard 191 errors are useful for statistical significance testing and drawing of inferential conclusions. 192

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The working of the Multiple Imputation method makes use of two main algorithms, namely
Expectation Maximization (EM) and Data Augmentation (DA). The procedure of data
imputation adopted in the study involves of the following steps:

- Step I: Data Transformation Firstly, it is required to transform the data to approximately normal before imputation using a transformation functions, such as logit, log or square root functions. After imputation, the data will be transformed back to their original scale.
- Step II: Imputation using EM EM uses the maximum likelihood approach to perform the imputation function in the "imputation and analysis phase" of the MI procedure.
 This step will generate estimates of missing values for the data matrix with the convergence criterion that the maximum relative parameter change in the value of any parameter during the iterative process is less than 10⁻⁶.
- Step III: Imputation using DA With the initial parameter estimates from the EM algorithm serving as the basis, the DA algorithm carries out multiple imputations as explained earlier in the "imputation and analysis phase" of the MI procedure. The commonly adopted practice of 10 imputations (14, 20) is applied in this study.
- Step IV: Synthesis of Estimates Average over the multiple estimates of the multiple imputation analysis to obtain the final set of estimates (17).
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213 ILLUSTRATIVE EXAMPLE: IMPUTATION OF ROUGHNESS DATA

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215 IRI Records in LTPP Database216

From the LTPP database (*16*) that provides measured records of pavement roughness data covering 24 years from 1989 to 2012, the following three records were extracted for the illustrative analysis of this study:

- Road Section SHRP ID 28-1802 with 8 years of continuous measured annual IRI (International Roughness Index) data;
- Road Section SHRP ID 20-1005 with 10 years of continuous measured annual IRI data;
 and
- Road Section SHRP ID 25-1002 with 16 years of continuous measured annual IRI data.

Table 1 records the measured IRI values and the corresponding times of measurements of the IRI records of the three road sections. These IRI data are plotted in Figure 1. Although the

annual IRI measurements were not measured at time intervals of exactly 12 months, they can

- be considered as time series data for the analysis and illustration purpose of the present example
- to study the effects of missing data.
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The three road sections have been selected because their pavement roughness variation trends display very distinctly different patterns. Road Sections SHRP ID 28-1802 and ID 20-1005 both had roughness value gradually increased with time, except for the latter there was a sharp drop in roughness value in the last year of the record. The roughness variations of Road Section ID 25-1002 were characterized by two periods of gentle increases (from year 1 to 7, and from year 12 to 15), two periods of sharp rises (from year 7 to 9, and from year 12 to 15), a period of sharp fall (from year 9 to 11) and a mild drop in year 16.

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240 Data Representation

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Pavement roughness is expected to increase with the number of years of service due to the 242 impact of traffic loading. However, in the occasion of pavement re-surfacing or rehabilitation, 243 the roughness would be restored to a lower value. Such maintenance and rehabilitation (M&R) 244 activities are common in road operations, they occurred for all three road sections considered 245 in the present study. As indicated in the LTPP database, for Road Section SHRP ID 28-1802, 246 minor M&R (maintenance and rehabilitation) took place in years 7 and 8 and resulted in slight 247 decreases in the IRI value. For Road Section ID 20-1005, a minor and a major M&R were 248 249 performed in years 5 and 10 respectively. For Road Section SHRP ID 25-1002, the database records indicated a major and a minor M&R in years 10 and 16 respectively. 250

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In the data imputation analysis, this situation was handled by introducing an M&R dummy variable. The dummy variable would be assigned a value of 1 if there was an M&R operation in the year of interest, and 0 otherwise. For the Road Section ID 25-1002, it is noted from Figure 1 that although the LTPP database indicated an M&R operation in year 11, a drop in the IRI value started to occur in year 10. It is suspected that part of the M&R might have commenced in year 10 and resulted in the fall of IRI.

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259 Generation of Datasets with Missing Data

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To study the effect of the proportion of missing data and determine the maximum allowable proportion of missing data, datasets with proportions of missing data ranging from approximately 10 to 90% were created for the three road sections studied. These datasets with missing data were randomly generated from the respective original complete data records of the three road sections. The levels of data missingness created for the three road sections studied are as follows:

- SHRP ID 28-1802: A total of 6 levels of data missingness was created. The percentages of missing data created were 12.5%, 25%, 37.5%, 50%, 62.5% and 75%;
 - SHRP ID 20-1005: A total of 8 levels of data missingness was created. The percentages of missing data created were 10%, 20%, 30%, 40%, 50%, 60%, 70% and 80%;
 - SHRP ID 25-1002: A total of 7 levels of data missingness was created. The percentages of missing data created were 12.5%, 25%, 37.5%, 50%, 62.5%, 75% and 87.5%.
- For each of the three road sections, at each level of data missingness, 10 different patterns of
 missing data were randomly created. Figures 2, 3 and 4 show all the patterns of missing data
 created for Road Sections SHRP ID 28-1802, SHRP ID 20-1005 and SHRP ID 25-1002
 respectively.

279 Analysis of Imputation Results

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281 <u>Error Analysis</u>

The error analysis involves examining the differences between the imputed data and the 283 284 corresponding actual data values of the original complete data records. As explained earlier, for each road section roughness record analyzed, 10 patterns of missing data were created for 285 each level of data missingness (see Figures 2 to 4); and for each pattern of missing data for a 286 287 given level of missingness, 10 imputation runs were made using the MI technique. Hence, there were 10 imputed values for each missing data form the 10 imputation runs, and the error 288 of each imputed roughness value is defined as its deviation from the actual roughness value of 289 290 the original complete data record.

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Figure 5 presents three examples of the mean and range of errors of the imputed values against 292 the levels of data missisngness (i.e. proportions of missing data) for the three road sections 293 studied. Figure 5(a) shows the results of imputation errors for the datasets of the level of data 294 missingness with 25% missing data for the roughness data of the Road Section SHRP ID 28-295 1802. At 25%, there were two missing data per dataset (i.e. two missing data per pattern of 296 missing data, see Figure 2). Hence, in Figure 5(a), there are two sets of error results for each 297 298 of the 10 patterns of missing patters. Similarly, in Figure 5(b) for the roughness data of Road Section SHRP ID 20-1005, there are two sets of error results for each of the 10 patterns of 299 300 missing patters at the level of missing data of 20%. For the roughness data of Road Section SHRP ID 25-1002, there are four sets of error results for each of the 10 patterns of missing 301 302 patters at the level of missing data of 25%.

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From the three plots of the errors of the imputed data values shown in Figure 5, the following comments can be made:

- 306 (1) For Road Section SHRP ID 28-1802, there are no clear trends of variation among the
 arrors for the 10 patterns. This is within expectation because the imputed data values
 were generated through a random process.
- 309 (2) For Road Section SHRP ID 20-1005, large errors are found for one imputed mean value
 and 6. These large errors occurred because the two patterns both
 contain a missing data in year 10, the year with a sudden drop in roughness value. This
 observation highlights that having missing data in regions of sharp changes in
 roughness data would introduce large errors when data imputation is applied.
- (3) For Road Section SHRP ID 25-1002, large errors occurred for one imputed mean value
 each for patterns 1, 5, 6, 8 and 10. Each of these patterns has a missing value in either
 year 9 or 10. These are the two years with a sharp fall of the roughness value. This
 observation reinforces the earlier observation made in the preceding paragraph
 concerning larger imputation errors associated with sharp changes in roughness data.
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Another error characteristic of interest is how errors vary with the level of data missingness. Figure 6 plots the mean and range of the absolute errors of imputed values against the levels of data missisngness (i.e. proportions of missing data) for all the cases of the three road sections studied. The following characteristics can be observed:

(1) For all three road sections, the magnitude of imputation errors increased with the level
 of data missingness. Road Section SHRP ID 28-1802 which has no abrupt changes in
 its roughness data, had the smallest mean imputation errors ranging from about 0.2 to

327 0.4 m/km; while the other two road sections containing abrupt changes in their
 328 roughness data, had larger mean imputation errors ranging from about 0.3 to 0.7 m/km.

- (2) The range of the errors was also found to increase with the level of data misisngness in general. Among the three road sections examined, the two road sections with abrupt changes in roughness data (i.e. SHRP ID 20-1005 and SHRP ID 25-1002) again displayed significantly larger ranges of variation in the range of the values of imputation mean.
- 335 <u>Reliability Analysis</u>

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The uncertainty involved in the imputation of missing values is reflected in the variations of the multiple imputed values for each missing data value of the example problem. Such variations are seen in the plots of Figures 5 and 6, where the distributions in the errors of imputed values as well as the variations among the means of different imputation runs, respectively, are depicted.

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With the error characteristics presented in Figures 5 and 6, a statistical reliability analysis of the imputation results can be performed. For the purpose of the present study, a hypothesis testing was performed to compare the mean computed value for each missing data with the corresponding actual data value of the original complete record. Since for each missing data, there were 10 imputed values, the Student's *t*-test (*21*) was employed for the test. The hypothesis testing considers the following null and alternative hypothesis:

Null hypothesis (H₀): The mean imputed value which is obtained from 10 imputation analyses, μ_z , is no different from the actual data value μ_0 from the original data record of the given road section, i.e.

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 $H_0: \mu_z = \mu_0$

Alternative hypothesis (H₁): The mean imputed value which is obtained from 10 imputation analyses, μ_z , is different from the actual data value μ_0 from the original data record of the given road section, i.e.

 $H_1: \mu_z \neq \mu_0$

For each data point in Figure 6, a hypothesis testing is performed for a given level of confidence to determine if the imputed mean value is different from the actual value. For a confidence level of 95%, Table 2 presents the results of the hypothesis test for all the cases of the three road sections studied. These results are plotted in Figure 7.

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From the results in Table 2 and Figure 7, taking a permissible error of 20% (i.e. corresponding 362 to the case of 80% "no difference" in Table 2) in the multiple imputation process, the maximum 363 allowable percentage of missing data is 30.3% for Road Section 28-1802, 20% for Road 364 Section 20-1005, and 18.75% for Road Section 25-1002. Thus, it appears reasonable for 365 practical application to set 25% as the limit of the proportion of missing data when there are 366 no abrupt changes of roughness data (i.e. no pavement rehabilitation) in the data records, and 367 apply a limit of 15% when the data records involve abrupt changes in roughness data caused 368 by pavement rehabilitation. 369

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371 Overall Comments

The error analysis presented in the preceding sections showed that imputation errors increased with the level of data missingness, and that abrupt changes in the data of the roughness records

- brought about by pavement resurfacing or rehabilitation would lead to increased errors in the

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- imputation results. As depicted in the plots of Figures 5 and 6, the increased errors due to
 rising levels of data missingness are also associated with increased variances of the imputed
 data. This implies that the reliability level of data imputation decreases as the level of data
 missingness increases.
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It was also observed that performing pavement rehabilitation within the analysis period, resulting in an abrupt fall in the roughness value in the data record, had a significant negative impact on the error magnitude and reliability of the imputed data. This can be expected because the action of rehabilitation caused a discontinuity in the deterioration trend of the roughness data. Based on the analysis presented, the following recommendations can be made regarding the maximum proportion of missing data allowable in the application of data imputation in pavement roughness analysis:

- (1) Allowing up to 20% error in the multiple imputation analysis at a confidence level of
 95%, 25% of missing data appears to be a reasonable allowable maximum limit for
 analyzing pavement roughness time series data not having any pavement
 rehabilitation within the analysis period. When pavement rehabilitation occurs within
 the analysis period, the maximum proportion of imputed data should be limited to
 15%.
- (2) Alternatively, a pre-processing before data imputation analysis may be performed to 394 a roughness data record that contains pavement rehabilitation operations. This pre-395 processing will break the original data record into one or more data records at the 396 year(s) of rehabilitation, so that each new sub-data record will contain roughness time 397 series data beginning after a year of construction/rehabilitation and ending before a 398 year of construction/rehabilitation. In this way, all new sub-data records will not 399 400 contain any rehabilitation within the analysis period, and the allowable maximum proportion of missing data can be set as 25% for in the data imputation analysis for all 401 sub-data records. 402
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404 CONCLUSIONS

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This paper has presented a procedure to evaluate the effect of the level of data missingness on the results of data imputation in pavement management analysis. A numerical example using pavement roughness data was presented to illustrate the proposed procedure and analyze the error and reliability characteristics of imputed data for three road sections. The roughness data of the three road sections were obtained from the LTPP database. From these data records, datasets with different proportions of missing data were randomly generated to study the effect of the level of data missingness.

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The analysis shows that the errors of imputed data increased with the level of data missingness, and their magnitudes are significantly affected by the effect of pavement rehabilitation. For the three road sections studied, the presence of rehabilitation within the period of the roughness record analysed caused the mean imputation errors to increase from a range of 0.2 to 0.4 m/km to about 0.3 to 0.7 m/km.

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Based on the examples analyzed, the study proposed maximum allowable proportions of
missing data for the application of data imputation in pavement roughness analysis. Allowing
up to 20% error in the multiple imputation analysis at a confidence level of 95%, the study
recommends 25% of missing data as a reasonable allowable maximum limit for analyzing

424 pavement roughness time series data not having any pavement rehabilitation within the analysis

425 period. When pavement rehabilitation occurs within the analysis period, the recommended426 maximum proportion of imputed data is 15%.

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The study also proposed performing of pre-processing of data record to eliminate the influence of pavement rehabilitation. This is achieved by breaking the data record into sub-records, each containing time series roughness data that begins from a year of rehabilitation and ends before the next rehabilitation year. By so doing, the maximum allowable limit of 25% missing data

- 432 can be uniformly applied to the imputation analysis of all data records.433

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SHRP ID	State	Year	Time of IRI measurement	IRI (m/km)		
		1	Aug 1990	0.895		
		2	May 1991	1.011		
		3	Aug 1992	1.163		
29, 1902		4	Jan 1993	1.251		
28-1802	MISISSISSIPPI	5	Aug 1994	1.722		
		6	Jul 1995	2.187		
		7	Apr 1996	2.142		
		8	Oct 1997	1.991		
		1	May 1992	2.933		
		2	Mar 1993	2.911		
		3	May 1994	2.833		
		4	Mar 1995	2.964		
20 1005	Vanaaa	5	Apr 1996	2.948		
20-1005	Kansas	6	Feb 1997	3.164		
		7	Apr 1998	3.369		
		8	Mar 1999	3.408		
		9	Feb 2000	3.448		
		10	May 2001	1.177		
		1	Oct 1989	1.164		
		2	Sep 1990	1.196		
		3	Jul 1991	1.189		
		4	Sep 1992	1.132		
		5	Sep 1993 1.186			
		6	Jan 1994	1.408		
		7	Jan 1995	1.607		
25 1002	Massachusatta	8	Nov 1996	2.198		
23-1002	wassachuseus	9	Jun 1997	3.387		
		10	Jun 1998	2.947		
		11	Jul 1999	1.451		
		12	Jun 2000	2.791		
		13	Apr 2001	2.844		
		14	Feb 2002	3.014		
	-	15	Sep 2003	3.245		
		16	Apr 2004	2.943		

TABLE 1 Observed IRI Values of Road Sections Studied

TABEL 2 Results of Hypothesis Testing of the Difference between Imputed IRI Values of Missing Data and Actual IRI Values

(a) Road Section ID 28-1802

	Difference between Imputed IRI Values and Actual Values at 95%					
Democrato es	Confidence Interval					
Missing Data	Number of Imputations	Number of Imputations	% Cases Showing			
Wiissing Data	Showing "No Difference	Showing "Significant	"No Difference in			
	in Results"	Difference in Results"	Results"			
12.5%	9	1	90.0			
25.0%	17	3	85.0			
37.5%	22	12	73.3			
50.0%	24	16	60.0			
62.5%	27	23	54.0			
75.0%	31	29	51.7			

(b) Road Section ID 20-1005

	Difference between Imputed IRI Values and Actual Values at 95%					
Deveentees	Confidence Interval					
Missing Data	Number of Imputations	Number of Imputations	% Cases Showing			
Missing Data	Showing "No Difference	Showing "Significant	"No Difference in			
	in Results"	Difference in Results"	Results"			
10%	9	1	90.0			
20%	16	4	80.0			
30%	21	9	70.0			
40%	25	15	62.5			
50%	29	21	58.0			
60%	30	30	50.0			
70%	34	36	48.6			
80%	38	42	47.5			

(c) Road Section ID 25-1002

	Difference between Imputed IRI Values and Actual Values at 955%					
Democrate co	Confidence Interval					
Missing Data	Number of Imputations	Number of Imputations	% Cases Showing			
Wilssing Data	Showing "No Difference	Showing "Significant	"No Difference in			
	in Results"	Difference in Results"	Results"			
12.5%	17	3	85			
25%	30	10	75			
37.5%	40	20	66.7			
50%	45	35	56.3			
62.5%	52	48	52.0			
75%	57	63	47.5			
87.5%	53	87	37.9			



FIGURE 1 Measured IRI Data of Road Sections Studied

13 50/		Percentage of Missing Data					
12.5%	25.0%	37.5%	50.0%	62.5%	75.0%		
1	1	0	1	0	0		
0	1	1	0	1	0		
1	1	0	1	0	1		
1	1	1	0	0	1		
1	0	1	1	1	0		
1	0	1	0	0	0		
1	1	0	1	0	0		
1	1	1	0	1	0		
	1 0 1 1 1 1 1 1 1 1	$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$		

Voor	Percentage of Missing Data					
rear	12.5%	25.0%	37.5%	50.0%	62.5%	75.0%
1	1	0	1	0	1	0
2	1	1	1	0	0	1
3	0	1	0	1	0	0
4	1	0	1	0	1	0
5	1	1	0	1	0	0
6	1	1	1	0	0	1
7	1	1	1	1	0	0
8	1	1	0	1	1	0
(c) Pattern 3						

Percentage of Missing Data

25.0% 37.5% 50.0% 62.5%

 Percentage of Missing Data

 12.5%
 25.0%
 37.5%
 50.0%
 62.5%

(i) Pattern 9

(g) Pattern 7

(e) Pattern 5

Percentage of Missing Data

25.0% 37.5% 50.0% 62.5%

75.0%

75.0%

75.0%

Year

Year

Year

12.5%

12.5%

Pattern 1

	7	1
	8	1
_		
_		

Year

12.5%

1	1	0	1
1	0	1	0
1	1	1	0
0	0	1	0
0	1	0	1

Percentage of Missing Data

1.01

25.0% 37.5% 50.0% 62.5%

75.0%

(a) Pattern 2

Vear		Percentage of Missing Data									
real	12.5%	25.0%	37.5%	50.0%	62.5%	75.0%					
1	1	0	0	1	0	1					
2	1	1	0	1	0	0					
3	1	0	1	0	1	0					
4	1	1	1	1	0	0					
5	1	1	0	0	0	1					
6	1	1	1	1	0	0					
7	0	1	1	0	1	0					
8	1	1	1	0	1	0					

(d) Pattern 4

Voar		Perc	centage of	f Missing	Data	
real	12.5%	25.0%	37.5%	50.0%	62.5%	75.0%
1	1	1	0	1	0	0
2	1	1	1	0	0	1
3	1	1	0	1	0	0
4	1	0	1	0	1	0
5	1	1	1	0	1	0
6	1	1	0	1	1	0
7	1	0	1	0	0	1
8	0	1	1	1	0	0

(f) Pattern 6

Voor		Perc	entage of	f Missing I	Data	
real	12.5%	25.0%	37.5%	50.0%	62.5%	75.0%
1	1	1	1	0	1	0
2	1	0	1	0	0	1
3	1	1	0	1	0	0
4	1	1	1	0	0	1
5	0	1	1	1	0	0
6	1	0	1	0	1	0
7	1	1	0	1	0	0
8	1	1	0	1	1	0

(h) Pattern 8

Voor		Perc	entage of	f Missing I	Data	
real	12.5%	25.0%	37.5%	50.0%	62.5%	75.0%
1	1	1	1	0	0	1
2	1	1	0	1	0	0
3	1	0	1	0	0	0
4	1	1	1	0	1	0
5	1	1	0	1	1	0
6	1	0	1	1	1	0
7	1	1	0	1	0	0
8	0	1	1	0	0	1
		(j) Patte	rn 10		





Voor			Percer	ntage of	f Missin	ig Data		
Teal	10%	20%	30%	40%	50%	60%	70%	80%
1	1	1	0	1	1	1	1	0
2	1	1	0	0	0	1	0	1
3	1	1	1	0	1	0	0	0
4	1	1	1	0	0	0	1	0
5	0	0	1	1	0	1	0	0
6	1	1	0	1	0	1	0	1
7	1	1	1	0	1	0	0	0
8	1	1	1	1	0	0	0	0
9	1	1	1	1	1	0	1	0
10	1	0	1	1	1	0	0	0

(a) Pattern 1

Voor			Percer	ntage of	f Missin	ig Data		
Teal	10%	20%	30%	40%	50%	60%	70%	80%
1	0	0	1	1	1	0	1	0
2	1	1	0	1	1	0	0	0
3	1	1	0	0	1	0	1	0
4	1	1	1	1	0	1	0	1
5	1	1	1	0	1	0	1	0
6	1	0	1	1	1	0	0	0
7	1	1	0	0	0	1	0	0
8	1	1	1	1	0	1	0	0
9	1	1	1	0	0	0	0	1
10	1	1	1	1	0	1	0	0

(c) Pattern 3

Vear			Percer	ntage of	f Missir	ng Data		
rear	10%	20%	30%	40%	50%	60%	70%	80%
1	1	1	0	0	0	1	0	1
2	1	1	0	0	1	0	0	0
3	1	0	1	1	0	1	1	1
4	1	1	1	1	1	0	0	0
5	1	1	1	1	0	1	0	0
6	1	1	1	0	1	1	0	0
7	1	1	1	1	0	0	1	0
8	1	0	1	1	1	0	0	0
9	1	1	0	1	0	0	1	0
10	0	1	1	0	1	0	0	0

(e) Pattern 5

Voor			Percer	ntage of	f Missin	ng Data		
real	10%	20%	30%	40%	50%	60%	70%	80%
1	1	1	1	1	1	0	0	0
2	1	0	1	1	1	1	1	0
3	1	1	1	1	1	0	0	0
4	1	1	0	0	0	1	0	0
5	1	1	1	0	1	0	1	0
6	1	1	1	0	1	0	1	0
7	0	0	1	1	0	0	0	1
8	1	1	1	0	0	1	0	0
9	1	1	0	1	0	0	0	0
10	1	1	0	1	0	1	0	1



Voar			Percer	ntage of	f Missir	ng Data				
Tear	10%	20%	30%	40%	50%	60%	70%	80%		
1	1	1	1	1	0	0	0	0		
2	1	1	1	1	1	0	1	1		
3	1	0	1	1	1	0	0	0		
4	0	1	0	0	1	0	0	0		
5	1	1	0	1	0	0	0	0		
6	1	1	0	1	1	1	0	0		
7	1	0	1	0	1	0	0	1		
8	1	1	1	1	0	1	1	0		
9	1	1	1	0	0	1	0	0		
10	1	1	1	0	0	1	1	0		
	(i) Pattern 9									

FIGURE 3 Patterns of Missing IRI Data Created for Road Section SHRP ID 20-1005

	•										
Voor			Percer	ntage of	f Missir	ig Data					
rear	10%	20%	30%	40%	50%	60%	70%	80%			
1	1	1	1	1	0	1	0	0			
2	1	0	1	1	0	0	0	0			
3	1	1	0	1	1	1	0	0			
4	1	1	1	0	0	0	1	0			
5	1	1	0	1	1	0	1	0			
6	1	1	1	1	0	0	0	0			
7	1	1	1	1	1	0	0	0			
8	0	1	0	0	1	0	1	1			
9	1	0	1	0	1	1	0	0			
10	1	1	1	0	0	1	0	1			
(b) Pattern 2											

 Percentage of Missing Data

 30%
 40%
 50%
 60%
 Year 10% 20% 70% 80%

(d) Pattern 4

Veer			Percer	ntage of	f Missin	ng Data				
rear	10%	20%	30%	40%	50%	60%	70%	80%		
1	1	1	1	0	1	0	0	0		
2	1	1	1	0	0	0	1	0		
3	1	1	1	1	0	1	0	0		
4	1	1	1	1	0	0	0	0		
5	1	1	0	1	0	1	0	0		
6	0	1	1	0	1	0	1	1		
7	1	1	1	1	0	1	1	0		
8	1	0	0	1	1	0	0	1		
9	1	1	1	0	1	1	0	0		
10	1	0	0	1	1	0	0	0		

(f) Pattern 6

Voor		Percentage of Missing Data										
rear	10%	20%	30%	40%	50%	60%	70%	80%				
1	1	1	1	1	0	0	1	0				
2	0	1	1	0	0	1	0	0				
3	1	1	0	0	0	0	1	0				
4	1	0	1	1	1	1	0	1				
5	1	0	1	0	1	1	0	1				
6	1	1	1	1	0	0	0	0				
7	1	1	0	1	1	0	0	0				
8	1	1	1	0	1	1	0	0				
9	1	1	0	1	0	0	1	0				
10	1	1	1	1	1	0	0	0				

(h) Pattern 8

/oor	Percentage of Missing Data								
ear	10%	20%	30%	40%	50%	60%	70%	80%	
1	1	1	1	0	0	0	0	1	
2	1	1	1	1	1	1	0	0	
3	1	1	1	1	0	1	0	0	
4	1	0	0	1	1	0	1	0	
5	1	1	1	0	1	0	0	1	
6	1	1	1	1	0	1	0	0	
7	1	1	1	1	0	1	1	0	
8	1	1	0	0	1	0	0	0	
9	0	0	1	1	1	0	0	0	
10	1	1	0	0	0	0	1	0	

(j) Pattern 10

Voor			Percenta	ge of Mis	sing Data		
rear	12.5%	25.0%	37.5%	50.0%	62.5%	75.0%	87.5%
1	1	1	0	1	0	0	1
2	1	1	1	0	1	0	0
3	1	1	1	0	1	0	0
4	1	1	0	0	1	0	0
5	1	0	1	1	0	0	1
6	0	1	0	0	1	0	0
7	1	1	1	0	0	1	0
8	1	0	1	1	0	0	0
9	1	0	1	0	0	1	0
10	1	1	0	0	1	0	0
11	1	0	0	1	0	0	0
12	1	1	0	1	0	1	0
13	1	1	1	1	0	0	0
14	1	1	1	0	1	0	0
15	0	1	1	1	0	0	0
16	1	1	1	1	0	1	0

Veer			Percenta	ge of Mis	sing Data		
Year	12.5%	25.0%	37.5%	50.0%	62.5%	75.0%	87.5%
1	1	0	1	1	1	0	0
2	1	1	0	0	1	0	0
3	1	1	1	0	0	1	0
4	1	0	1	0	1	0	0
5	0	1	0	1	0	0	0
6	1	1	1	0	1	0	0
7	1	1	0	1	0	0	1
8	1	1	0	1	0	0	1
9	1	1	0	1	1	0	0
10	0	1	1	1	0	0	0
11	1	0	1	0	0	1	0
12	1	1	1	0	0	1	0
13	1	1	0	0	1	0	0
14	1	1	1	1	0	0	0
15	1	0	1	0	0	1	0
16	1	1	1	1	0	0	0

(a) Pattern 1

Percentage of Missing Data 37.5% 50.0% 62.5% Year 25.0% 87.5% 12.5% 75.0%

(c)	Pattern	3
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	_

Voor			Percenta	ge of Mis	sing Data		
rear	12.5%	25.0%	37.5%	50.0%	62.5%	75.0%	87.5%
1	1	1	0	1	0	0	0
2	1	1	1	1	0	0	0
3	0	0	1	0	1	0	0
4	1	1	1	1	0	0	1
5	1	1	0	1	0	0	0
6	1	1	1	0	0	1	0
7	1	1	1	0	0	1	0
8	1	1	0	0	1	0	0
9	0	1	1	0	1	0	0
10	1	0	0	1	1	0	0
11	1	1	1	0	0	1	0
12	1	1	1	0	0	1	0
13	1	1	1	1	0	0	0
14	1	0	0	1	1	0	0
15	1	1	0	1	0	0	1
16	1	0	1	0	1	0	0
			(e) Pa	ttern 5			

(b) Pattern 2

		Percenta	ge of Mis	sing Data		
12.5%	25.0%	37.5%	50.0%	62.5%	75.0%	87.5%
1	1	1	0	1	0	0
1	1	0	1	0	0	1
1	0	1	0	1	0	0
1	1	1	0	0	1	0
1	1	0	0	1	0	0
1	0	1	1	0	0	0
1	1	0	0	1	0	0
1	1	1	0	1	0	0
1	1	0	1	0	0	0
1	1	0	1	0	1	0
0	0	1	0	0	1	0
1	1	1	1	0	0	0
1	1	1	1	0	0	1
1	0	1	1	0	0	0
0	1	0	0	1	0	0
1	1	1	1	0	1	0
	12.5% 1 1 1 1 1 1 1 1 1 1 1 1 1	12.5% 25.0% 1 1 1 1 1 0 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 0 0 1 1 1 1 0 0 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	Percenta 12.5% 25.0% 37.5% 1 1 1 1 1 0 1 0 1 1 1 0 1 1 1 1 1 0 1 1 0 1 1 0 1 1 0 1 1 0 1 1 0 1 1 0 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 0 1 1 0 1 1 0 1 1 0 1 1 1 0 1 1 1	Percentage of Mis 12.5% 25.0% 37.5% 50.0% 1 1 1 0 1 1 0 1 1 0 1 0 1 1 0 1 1 0 1 0 1 1 0 0 1 1 0 0 1 1 0 0 1 1 0 1 1 1 0 1 1 1 0 1 1 1 0 1 1 1 0 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	Percentage of Missip Data 12.5% 25.0% 37.5% 50.0% 62.5% 1 1 0 1 1 1 0 1 1 1 0 1 0 1 1 0 1 0 1 1 0 1 0 1 1 0 1 0 1 1 0 0 1 1 0 1 1 0 1 1 0 1 1 1 0 1 1 0 1 1 0 1 0 1 1 0 1 0 0 1 1 0 1 0 0 0 1 1 1 1 0 0 0 0 1 1 0 1 0 0 0 0	Percentage of Missing Data 12.5% 25.0% 37.5% 50.0% 62.5% 75.0% 1 1 1 0 1 0 1 1 0 1 0 1 0 1 1 0 1 0 1 0 1 1 0 1 0 1 0 1 1 0 1 0 1 0 1 1 0 0 1 0 0 1 1 0 1 1 0 0 1 0 1 1 0 0 1 0 0 1 0 0 1 0 0 1 0 0 1 0 1 0 0 1 0 0 1 0 1 0 1 0 1 0 1 1 0 1 1 1

(d) Pattern 4

Voor			Percenta	ge of Mis	sing Data		
rear	12.5%	25.0%	37.5%	50.0%	62.5%	75.0%	87.5%
1	1	1	1	1	0	0	0
2	1	0	1	1	0	1	0
3	1	0	1	0	1	0	0
4	1	0	1	0	0	1	0
5	0	1	1	1	0	0	0
6	1	1	1	0	1	0	0
7	0	1	0	1	0	0	0
8	1	1	0	0	1	0	1
9	1	0	1	1	0	0	0
10	1	1	1	0	1	0	0
11	1	1	0	1	0	1	0
12	1	1	0	0	1	0	0
13	1	1	1	0	1	0	0
14	1	1	1	0	0	1	0
15	1	1	0	1	0	0	0
16	1	1	0	1	0	0	1
					-		

(f) Pattern 6

FIGURE 4 Patterns of Missing IRI Data Created for Road Section SHRP ID 25-1002 (continued next page)

Voor			Percenta	ge of Mis	sing Data			Voor			Percenta	ge of Mis	sing Data		
rear	12.5%	25.0%	37.5%	50.0%	62.5%	75.0%	87.5%	rear	12.5%	25.0%	37.5%	50.0%	62.5%	75.0%	87.5%
1	1	1	0	0	1	0	0	1	1	0	1	0	1	0	0
2	1	1	0	1	0	0	0	2	1	1	0	1	0	0	1
3	1	1	1	0	0	1	0	3	1	1	0	1	0	0	0
4	1	1	1	1	0	0	0	4	0	1	1	0	0	1	0
5	0	0	1	0	0	0	1	5	1	1	1	0	0	1	0
6	1	0	1	1	1	0	0	6	1	1	0	0	1	0	0
7	1	0	0	1	0	0	0	7	0	1	0	1	0	0	1
8	0	1	1	0	0	1	0	8	1	1	1	1	0	0	0
9	1	1	0	1	1	0	0	9	1	0	1	0	0	1	0
10	1	1	1	0	0	1	0	10	1	1	0	1	1	0	0
11	1	1	1	1	0	0	0	11	1	0	1	1	0	0	0
12	1	0	1	0	0	1	0	12	1	1	1	0	0	1	0
13	1	1	1	1	0	0	1	13	1	0	1	1	0	0	0
14	1	1	0	0	1	0	0	14	1	1	1	1	1	0	0
15	1	1	0	0	1	0	0	15	1	1	0	0	1	0	0
16	1	1	1	1	1	0	0	16	1	1	1	0	1	0	0
			(g) Pa	ttern 7							(h) Patt	ern 8		
Vee			Percenta	ge of Mis	sing Data			Veer			Percenta	ge of Mis	sing Data		
Year	12.5%	25.0%	Percenta 37.5%	ge of Mis 50.0%	sing Data 62.5%	75.0%	87.5%	Year	12.5%	25.0%	Percenta 37.5%	ge of Mis 50.0%	sing Data 62.5%	75.0%	87.5%
Year 1	12.5% 1	25.0% 1	Percenta 37.5%	ge of Mis 50.0% 1	sing Data 62.5% 1	75.0% 0	87.5% 0	Year 1	12.5% 0	25.0% 0	Percenta 37.5%	ge of Mis 50.0% 0	sing Data 62.5% 0	75.0% 1	87.5% 0
Year 1 2	12.5% 1 1	25.0% 1 1	Percenta 37.5% 0 1	ge of Mis 50.0% 1 0	sing Data 62.5% 1 0	75.0% 0 1	87.5% 0 0	Year 1 2	12.5% 0 1	25.0% 0 1	Percenta 37.5% 1 0	ge of Mis 50.0% 0 1	sing Data 62.5% 0 0	75.0% 1 0	87.5% 0 0
Year 1 2 3	12.5% 1 1 0	25.0% 1 1 1	Percenta 37.5% 0 1 0	ge of Mis 50.0% 1 0 1	sing Data 62.5% 1 0 0	75.0% 0 1 0	87.5% 0 0 0	Year 1 2 3	12.5% 0 1 1	25.0% 0 1 1	Percenta 37.5% 1 0 1	ge of Mis 50.0% 0 1 0	sing Data 62.5% 0 0 0	75.0% 1 0 1	87.5% 0 0 0
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FIGURE 4 Patterns of Missing IRI Data Created for Road Section SHRP ID 25-1002 (continuation)



FIGURE 5 Mean and Ranges of Errors of Imputation Results for Road Sections Studied



FIGURE 6 Mean Errors of Imputation Data against Level of Data Missingness



FIGURE 7 Effect of Proportion of Missing Data on Imputation Results