

LAMPIRAN 2 Perhitungan Torsi, daya, dan efisiensi turbin Darrieus NACA 0012

2.1 Perhitungan Torsi

- Kecepatan 2

Dik:

$$U = 2 \text{ m/s} \quad \omega = 29.23 \text{ rad/s} \quad C_{L1} = 1.142 \sin(2.065x)$$

$$H = 0.8 \text{ m} \quad \rho = 998.2 \text{ kg/m}^3 \quad C_{L2} = 1.749 \sin(2.435x)$$

$$c = 0.18 \text{ m} \quad R = 0.3 \text{ m} \quad C_D = 1.145 \sin(0.2695x + 1.571) + 1.13 \sin(4.611x - 1.571)$$

Torsi Lift

$$\frac{1}{\pi} \int_{-\frac{\pi}{2}}^{\frac{\pi}{2}} \rho(0.5)(W)^2 A. CL. (R \sin(x)) dx + \frac{1}{\pi} \int_{\frac{\pi}{2}}^{\frac{3\pi}{2}} \rho(0.5)(W)^2 A. CL. (R \sin(x)) dx$$

2

Sudu 1

$$T_{L1} = \frac{1}{\pi} \left(\int_{-\frac{\pi}{2}}^{\frac{\pi}{2}} \rho(0.5)(W)^2 A. CL. (R \sin(x)) dx \right)$$

$$= \frac{1}{\pi} \left(\int_{-\frac{\pi}{2}}^{\frac{\pi}{2}} 998.2(0.5)(U + (-\omega R))^2 (H)(c)(1.142 \sin(2.065x))(R \sin(x)) dx \right)$$

$$\begin{aligned}
&= \frac{1}{\pi} \left(\int_{-\frac{\pi}{2}}^{\frac{\pi}{2}} 998.2(0.5)(2 + ((-29.23)(0.3))^2)(0.8)(0.18)(1.142\sin(2.065x))(0.3 \sin(x)) dx \right) \\
&= \frac{1}{\pi} \cdot 998.2(0.5)(2 + ((-29.23)(0.3))^2)(1.142)(0.8)(0.18)(0.3) \int_{-\frac{\pi}{2}}^{\frac{\pi}{2}} \sin(x)\sin(2.065x) dx \\
&= \frac{1}{\pi} (499.1)(45.819)(1.142)(0.8)(0.18)(0.3) \int_{-\frac{\pi}{2}}^{\frac{\pi}{2}} \sin(x)\sin(2.065x) dx \\
&= 359.115 \int_{-\frac{\pi}{2}}^{\frac{\pi}{2}} \sin(x)\sin(2.065x) dx \\
&= (351.115)(1.259) \\
&= 452.126 \text{ Nm}
\end{aligned}$$

$$\begin{aligned}
T_{L2} &= \frac{1}{\pi} \left(\int_{\frac{\pi}{2}}^{\frac{3\pi}{2}} \rho(0.5)(W)^2 A. CL. (R\sin(x)) dx \right) \\
&= \frac{1}{\pi} \left(\int_{\frac{\pi}{2}}^{\frac{3\pi}{2}} 998.2(0.5)(U + (-\omega R))^2 (H)(c)(1.749\sin(2.435x))(0.3 \sin(x)) dx \right) \\
&= \frac{1}{\pi} (499.1)(45.819)(1.749)(0.8)(0.18)(0.3) \left(\int_{\frac{\pi}{2}}^{\frac{3\pi}{2}} \sin(2.435x)\sin(x) dx \right) \\
&= 549.993 \left(\int_{\frac{\pi}{2}}^{\frac{3\pi}{2}} \sin(2.435x)\sin(x) dx \right)
\end{aligned}$$

$$= (549.993) (-0.2)$$

$$= -109.999 \text{ Nm}$$

Sudu 2

$$T_{L1} = \frac{1}{\pi} \left(\int_{-\frac{\pi}{2}}^{\frac{\pi}{2}} 998.2(0.5)(2 + ((-29.23)(0.3))^2(H)(c) \left(1.142 \sin \left(2.065 \left(x + \frac{2\pi}{3} \right) \right) \right) (0.3 \sin(x + 2\pi/3)) dx \right)$$

$$= (351.115) \int_{-\frac{\pi}{2}}^{\frac{\pi}{2}} \sin(x + 2\pi/3) \sin(2.065x + 1.376\pi) dx$$

$$= ((351.115)) (-0.249)$$

$$= -87.428 \text{ Nm}$$

$$T_{L2} = \frac{1}{\pi} \left(\int_{\frac{\pi}{2}}^{\frac{3\pi}{2}} 998.2(0.5)(2 + ((-29.23)(0.3))^2(H)(c) (1.749 \sin(2.435(x + 2\pi/3))) (0.3 \sin(x + 2\pi/3)) dx \right)$$

$$= 549.993 \left(\int_{\frac{\pi}{2}}^{\frac{3\pi}{2}} \sin(2.435x + 1.623\pi) \sin((x + 2\pi/3)) dx \right)$$

$$= (549.993) \cdot (0.327)$$

$$= 179.848 \text{ Nm}$$

Sudu 3

$$\begin{aligned} T_{L1} &= \frac{1}{\pi} \left(\int_{-\frac{\pi}{2}}^{\frac{\pi}{2}} 998.2(0.5)(2 + ((-29.23)(0.3))^2(H)(c) \left(1.142 \sin \left(2.065 \left(x + \frac{4\pi}{3} \right) \right) \right) (0.3 \sin(x + 4\pi/3)) dx \right) \\ &= (351.115) \int_{-\frac{\pi}{2}}^{\frac{\pi}{2}} \sin(x + 4\pi/3) \sin(2.065x + 2.753\pi) dx \\ &= ((351.115))(0.079) \\ &= 27.738 \text{ Nm} \end{aligned}$$

$$\begin{aligned} T_{L2} &= \frac{1}{\pi} \left(\int_{\frac{\pi}{2}}^{\frac{3\pi}{2}} 998.2(0.5)(2 + ((-29.23)(0.3))^2(H)(c) (1.749 \sin(2.435(x + 4\pi/3))) (0.3 \sin(x + 4\pi/3)) dx \right) \\ &= (550) \left(\int_{\frac{\pi}{2}}^{\frac{3\pi}{2}} \sin(2.435x + 3.246\pi) \sin((x + 4\pi/3)) dx \right) \\ &= (549.993)(-0.023) \\ &= -12.65 \text{ Nm} \end{aligned}$$

$$\begin{aligned}
T_L \text{ total} &= ((T_{L1\text{sudu1}} + T_{L2\text{sudu1}}) + (T_{L1\text{sudu2}} + T_{L2\text{sudu2}}) + (T_{L1\text{sudu3}} + T_{L2\text{sudu3}}))/2 \\
&= \frac{(452.126 - 109.999) + (-87.428 + 179.848) + (27.738 - 12.65)}{2} \\
&= 224.818 \text{ Nm}
\end{aligned}$$

Torsi Drag

Sudu 1

$$\begin{aligned}
T_D &= \frac{1}{2\pi} \int_0^{2\pi} \rho(0.5)(W)^2 A \cdot CD \cdot (R \cos(x)) dx \\
&= \frac{1}{2\pi} \int_0^{2\pi} (\rho)(0.5)(2 + ((-29.23)(0.3))^2(A) (1.145 \sin(0.2695 x + 1.571) + 1.13 \sin(4.611x - 1.571))(0.3 \cos(x)) dx \\
&= \frac{1}{2\pi} (998.2)(0.5)(45.819)(0.3)(0.8)(0.18) \int_0^{2\pi} (1.145 \sin(0.2695 x + 1.571) + 1.13 \sin(4.611x - 1.571))(\cos(x)) dx \\
&= 157.231 \int_0^{2\pi} (1.145 \sin(0.2695 x + 1.571)) (\cos(x)) + (1.13 \sin(4.611x - 1.571))(\cos(x)) dx \\
&\quad \int_0^{2\pi} (1.145 \sin(0.2695 x + 1.571)) (\cos(x)) + (1.13 \sin(4.611x - 1.571))(\cos(x)) dx \\
&\quad \int_0^{2\pi} (\sin(\alpha)(\cos(\beta)) dx \quad \alpha = 40.2695 x + 1.571, \quad \beta = x, \quad \alpha = 44.611x - 1.571 \\
&\quad \int_0^{2\pi} \frac{1}{2} (\sin(\alpha - \beta) + (\sin(\alpha + \beta)) dx \\
&= 157.231 \int_0^{2\pi} \frac{1}{2} 1.145 ((\sin(1.2695 x + 1.571) + (\sin(-0.731 x + 1.571))) dx + \int_0^{2\pi} \frac{1}{2} 1.13 ((\sin(3.611 x - 1.571) + (\sin(5.611 x - 1.571))) dx
\end{aligned}$$

$$\begin{aligned}
&= 157.231 \int_0^{2\pi} \frac{1}{2} 1.145 ((\sin(1.27x + 0.00643\pi) + \sin(-0.73x + 0.00643\pi))) dx + \int_0^{2\pi} \frac{1}{2} 1.13 ((\sin(3.61x - 0.00643\pi) + \sin(5.61x - 0.00643\pi))) dx \\
&= (157.231)(0.081) \\
&= 12.736 \text{ Nm}
\end{aligned}$$

Sudu 2

$$\begin{aligned}
T_D &= \frac{1}{2\pi} \int_0^{2\pi} (998.2)(0.5)(45.819)(0.3)(0.8)(0.18) (1.145 \sin(0.2695(x + \frac{2\pi}{3}) + 1.571) + 1.13 \sin(4.611(x + \frac{2\pi}{3}) - 1.571)) (0.3 \cos(x + \frac{2\pi}{3})) dx \\
&= 157.231 \int_0^{2\pi} (1.145 \sin(0.2695x + 0.186\pi) + 1.13 \sin(4.611x + 3.068\pi)) \cos(x + \frac{2\pi}{3}) dx \\
&= 157.231 \int_0^{2\pi} 1.145 (\sin(0.2695x + 0.186\pi) \cos(x + \frac{2\pi}{3}) + 1.13 \sin(4.611x + 3.068\pi) \cos(x + \frac{2\pi}{3})) dx \\
&= 157.231 \int_0^{2\pi} \frac{1}{2} 1.145 ((\sin(1.2695x + 0.856\pi) + \sin(-0.731x - 0.484\pi))) dx + \int_0^{2\pi} \frac{1}{2} 1.13 ((\sin(3.611x + 2.398\pi) + \sin(5.611x + 3.738\pi))) dx \\
&= (157.231)(0.633) \\
&= 99.527 \text{ Nm}
\end{aligned}$$

Sudu 3

$$\begin{aligned}T_D &= \frac{1}{2\pi} \int_0^{2\pi} (998.2)(0.5)(45.819)(0.3)(0.8)(0.18) \left(1.145 \sin \left(0.2695 \left(x + \frac{4\pi}{3} \right) + 1.571 \right) + 1.13 \sin \left(4.611 \left(x + \frac{4\pi}{3} \right) - 1.571 \right) \right) \left(0.3 \cos \left(x + \frac{4\pi}{3} \right) \right) dx \\&= 157.231 \int_0^{2\pi} \left(1.145 \sin(0.2695x + 0.365\pi) + 1.13 \sin(4.611x + 6.126\pi) \right) \cos \left(x + \frac{4\pi}{3} \right) dx \\&= 157.231 \int_0^{2\pi} 1.145 \sin(0.2695x + 0.365\pi) \cos \left(x + \frac{4\pi}{3} \right) + 1.13 \sin(4.611x + 6.126\pi) \cos \left(x + \frac{4\pi}{3} \right) dx \\&= 157.231 \int_0^{2\pi} \frac{1}{2} 1.145 \left(\sin(1.2695x + 1.695\pi) + \sin(-0.731x - 0.965\pi) \right) dx + \int_0^{2\pi} \frac{1}{2} 1.13 \left(\sin(3.611x + 4.796\pi) + \sin(5.611x + 7.456\pi) \right) dx \\&= (157.231)(0.639) \\&= 100.471 \text{ Nm}\end{aligned}$$

$$\begin{aligned}T_D \text{ total} &= (T_{Dsudu1} + T_{Dsudu2} + T_{Dsudu3}) \\&= 12.736 + 99.527 + 100.471 \\&= 212.734 \text{ Nm}\end{aligned}$$

$$\begin{aligned}T_{\text{TOTAL}} &= (T_L \text{ total} - T_D \text{ total}) \\&= (224.818) - (212.734) \\&= 12.084 \text{ Nm}\end{aligned}$$

Kecepatan 2.5 m/s

Dik:

$$U = 2.5 \text{ m/s} \quad \omega = 37.738 \text{ rad/s} \quad C_{L1} = 1.29 \sin(2.11x)$$

$$H = 0.8 \text{ m} \quad \rho = 998.2 \text{ kg/m}^3 \quad C_{L2} = 1.745 \sin(2.417x)$$

$$c = 0.18 \text{ m} \quad R = 0.3 \text{ m} \quad C_D = 1.157 \sin(0.2497x + 1.571) + 1.143 \sin(4.631x - 1.571)$$

Torsi Lift

Sudu 1

$$\begin{aligned} T_{L1} &= \frac{1}{\pi} \left(\int_{-\frac{\pi}{2}}^{\frac{\pi}{2}} \rho (0.5) (W)^2 A \cdot C_{L1} \cdot (R \sin(x)) dx \right) \\ &= \frac{1}{\pi} \left(\int_{-\frac{\pi}{2}}^{\frac{\pi}{2}} 998.2 (0.5) (U + (-\omega R))^2 (H) (c) (1.29 \sin(2.11x)) (0.3 \sin(x)) dx \right) \\ &= \frac{1}{\pi} \left(\int_{-\frac{\pi}{2}}^{\frac{\pi}{2}} 998.2 (0.5) (2.5 + ((-37.738)(0.3)))^2 (0.8) (0.18) (1.29 \sin(2.11x)) (0.3 \sin(x)) dx \right) \\ &= \frac{1}{\pi} \cdot 998.2 (0.5) (2.5 + ((-37.738)(0.3)))^2 (0.8) (0.18) (1.29) (0.3) \int_{-\frac{\pi}{2}}^{\frac{\pi}{2}} \sin(x) \sin(2.11x) dx \\ &= \frac{1}{\pi} (499.1) (81.046) (0.8) (0.18) (1.29) (0.3) \int_{-\frac{\pi}{2}}^{\frac{\pi}{2}} \sin(x) \sin(2.11x) dx \end{aligned}$$

$$= (717.534)(1)$$

$$= 861 \text{ Nm}$$

$$T_{L2} = \frac{1}{\pi} \left(\int_{\frac{\pi}{2}}^{\frac{3\pi}{2}} \rho(0.5)(W)^2 A. CL2. (R \sin(x)) dx \right)$$

$$T_{L2} = \frac{1}{\pi} \left(\int_{\frac{\pi}{2}}^{\frac{3\pi}{2}} 998.2(0.5)(U + (-\omega R))^2 (H)(c)(1.745 \sin(2.417x))(0.3 \sin(x)) dx \right)$$

$$T_{L2} = \frac{1}{\pi} (499.1)(81.046)(0.8)(0.18)(1.745)(0.3) \left(\int_{\frac{\pi}{2}}^{\frac{3\pi}{2}} \sin(2.417x) \sin(x) dx \right)$$

$$T_{L2} = (970.618)(-0.21)$$

$$T_{L2} = -203.8 \text{ Nm}$$

Sudu 2

$$T_{L1} = \frac{1}{\pi} \left(\int_{-\frac{\pi}{2}}^{\frac{\pi}{2}} 998.2(0.5)(2.5 + ((-37.738)(0.3))^2 (H)(c) \left(1.29 \sin \left(2.11 \left(x + \frac{2\pi}{3} \right) \right) \right) (0.3 \sin(x + 2\pi/3)) dx \right)$$

$$= (717.534) \int_{-\frac{\pi}{2}}^{\frac{\pi}{2}} \sin(x + 2\pi/3) \sin(2.11x + 1.41\pi) dx$$

$$= (717.534) (-0.31)$$

$$= -222.4 \text{ Nm}$$

$$T_{L2} = \frac{1}{\pi} \left(\int_{\frac{\pi}{2}}^{\frac{3\pi}{2}} 998.2(0.5)(2.5 + ((-136.9231)(0.3))^2(H)(c)(1.745\sin(2.417(x + 2\pi/3)))(0.3 \sin(x + 2\pi/3))dx \right)$$

$$= (970.618) \left(\int_{\frac{\pi}{2}}^{\frac{3\pi}{2}} \sin(2.435x + 1.611\pi)\sin((x+2\pi/3))dx \right)$$

$$= (970.618)(0.33)$$

$$= 320.304 \text{ Nm}$$

Sudu 3

$$T_{L1} = \frac{1}{\pi} \left(\int_{-\frac{\pi}{2}}^{\frac{\pi}{2}} 998.2(0.5)(2.5 + ((-37.738)(0.3))^2c \left(1.29\sin \left(2.11(x + \frac{4\pi}{3}) \right) \right) (0.3 \sin(x + 4\pi/3))dx \right)$$

$$= (717.534) \int_{-\frac{\pi}{2}}^{\frac{\pi}{2}} \sin(x+4\pi/3)\sin(2.11x+2.813\pi)dx$$

$$= (717.534) (0.2)$$

$$= 143.50 \text{ Nm}$$

$$\begin{aligned}
T_{L2} &= \frac{1}{\pi} \left(\int_{\frac{\pi}{2}}^{\frac{3\pi}{2}} 998.2(0.5)(2.5 + ((-37.738)(0.3))^2 c(1.745 \sin(2.417(x + 4\pi/3)))(0.3 \sin(x + 4\pi/3)) dx \right) \\
&= (485.309) \left(\int_{\frac{\pi}{2}}^{\frac{3\pi}{2}} \sin(2.417x + 3.223\pi) \sin((x+4\pi/3)) dx \right) \\
&= (970.618)(-0.088) \\
&= -85.414 \text{ Nm}
\end{aligned}$$

$$\begin{aligned}
T_L \text{ total} &= ((T_{L1sudu1} + T_{L2sudu1}) + (T_{L1sudu2} + T_{L2sudu2}) + (T_{L1sudu3} + T_{L2sudu3}))/2 \\
&= \frac{(657.2) + (-222.283 + 320.304) + (143.5 - 85.414)}{2} \\
&= 406.65 \text{ Nm}
\end{aligned}$$

Torsi Drag

Sudu 1

$$\begin{aligned}T_D &= \frac{1}{2\pi} \int_0^{2\pi} \rho(0.5)(W)^2 A. CD. (R \cos(x)) dx \\&= \frac{1}{2\pi} \int_0^{2\pi} (\rho)(0.5)(2.5 + ((-37.738)(0.3))^2(H)(c)(1.157 \sin(0.2497x + 1.571) + 1.143 \sin(4.631x - 1.571))(0.3 \cos(x)) dx \\&= \frac{1}{2\pi} (998.2)(0.5)(81.046)(0.8)(0.18)(0.3) \int_0^{2\pi} ((1.157 \sin(0.2497x + 1.571) + 1.143 \sin(4.631x - 1.571))(\cos(x)) dx \\&= 278.114 \int_0^{2\pi} 1.157 \sin(0.2497x + 1.571) (\cos(x)) + (1.143 \sin(4.631x - 1.571))(\cos(x)) dx \\&= 278.114 \int_0^{2\pi} \frac{1}{2} 1.157 ((\sin(1.2497x + 1.571) + (\sin(-0.7503x + 1.571))) dx + \int_0^{2\pi} \frac{1}{2} 1.143 ((\sin(3.631x - 1.571) + (\sin(5.631x - 1.571))) dx \\&= (278.114)(0.13) \\&= 13.268 Nm\end{aligned}$$

Sudu 2

$$\begin{aligned}T_D &= \frac{1}{2\pi} \int_0^{2\pi} (998.2)(0.5)(81.046)(0.8)(0.18)(1.157 \sin(0.2497(x + \frac{2\pi}{3}) + 1.571) + 1.143 \sin(4.631(x + \frac{2\pi}{3}) - 1.571)) (0.3 \cos(x + \frac{2\pi}{3})) dx \\&= 278.114 \int_0^{2\pi} (1.157 \sin(0.2497x + 0.173\pi) + 1.143 \sin(4.631x + 3.087\pi)) \cos(x + \frac{2\pi}{3}) dx\end{aligned}$$

$$\begin{aligned}
&= 278.114 \int_0^{2\pi} 1.157(\sin(0.2497x + 0.173\pi)\cos(x + \frac{2\pi}{3}) + 1.143\sin(4.631x + 3.087\pi)\cos(x + \frac{2\pi}{3}))dx \\
&= 278.114 \int_0^{2\pi} \frac{1}{2} 1.157((\sin(1.2497x + 0.833\pi) + (\sin(-0.75x - 0.487\pi)))dx + \int_0^{2\pi} \frac{1}{2} 1.143((\sin(3.631x + 2.421\pi) + (\sin(5.631x + 3.753\pi)))dx \\
&= (278.114)(0.681) \\
&= 189.396Nm
\end{aligned}$$

Sudu 3

$$\begin{aligned}
T_D &= \frac{1}{2\pi} \int_0^{2\pi} (998.2)(0.5)(81.046)(0.8)(0.1)(1.157\sin(0.2497(x + \frac{4\pi}{3}) + 1.571) + 1.143\sin(4.631(x + \frac{4\pi}{3}) - 1.571(0.3\cos(x + \frac{4\pi}{3})))dx \\
&= 278.114 \int_0^{2\pi} (1.157\sin(0.2497x + 0.339\pi) + 1.143\sin(4.631x + 9.268\pi)\cos(x + \frac{4\pi}{3}))dx \\
&= 278.114 \int_0^{2\pi} 1.157\sin(0.2497x + 0.339\pi)\cos(x + \frac{4\pi}{3}) + 1.143\sin(4.631x + 9.268\pi)\cos(x + \frac{4\pi}{3})dx \\
&= 278.114 \int_0^{2\pi} \frac{1}{2} 1.157((\sin(1.2497x + 1.669\pi) + (\sin(-0.75x - 0.994\pi)))dx + \int_0^{2\pi} \frac{1}{2} 1.143((\sin(3.631x + 7.935\pi) + (\sin(5.631x + 10.601\pi)))dx \\
&= (278.114)(0.647) \\
&= 179.94Nm
\end{aligned}$$

$$\begin{aligned}T_D \text{ total} &= (T_{Dsudu1} + T_{Dsudu2} + T_{Dsudu3}) \\ &= 13.268 + 189.396 + 179.94 \\ &= 382.604 \text{ Nm}\end{aligned}$$

$$\begin{aligned}T_{TOTAL} &= (T_{Ltotal} + T_{Dtotal}) \\ &= (406.65) - (382.604) \\ &= 24.05 \text{ Nm}\end{aligned}$$

Kecepatan 3 m/s

Dik:

$$U = 3 \text{ m/s}$$

$$\omega = 46.246 \text{ rad/s}$$

$$C_{L1} = 1.265 \sin(2.124x)$$

$$H = 0.8 \text{ m}$$

$$\rho = 998.2 \text{ kg/m}^3$$

$$C_{L2} = 1.745 \sin(2.417x)$$

$$c = 0.18 \text{ m}$$

$$R = 0.3 \text{ m}$$

$$C_D = 1.171 \sin(0.2409x + 1.571) + 1.157 \sin(4.639x - 1.571)$$

Torsi Lift

Sudu 1

$$T_{L1} = \frac{1}{\pi} \left(\int_{-\frac{\pi}{2}}^{\frac{\pi}{2}} \rho (0.5) (W)^2 A \cdot C_{L1} \cdot (R \sin(x)) dx \right)$$

$$= \frac{1}{\pi} \left(\int_{-\frac{\pi}{2}}^{\frac{\pi}{2}} 998.2 (0.5) (U + (-\omega R))^2 (H) (c) (1.265 \sin(2.124x)) (0.3 \sin(x)) dx \right)$$

$$= \frac{1}{\pi} \left(\int_{-\frac{\pi}{2}}^{\frac{\pi}{2}} 998.2 (0.5) (3 + ((-46.246)(0.3))^2) (0.8) (0.18) (1.265 \sin(2.124x)) (0.3 \sin(x)) dx \right)$$

$$= \frac{1}{\pi} (499.1) (118.244) (0.8) (0.18) (1.265) (0.3) \int_{-\frac{\pi}{2}}^{\frac{\pi}{2}} \sin(x) \sin(2.124x) dx$$

$$= (1026.58) (1.186)$$

$$= 1217.52 \text{ Nm}$$

$$\begin{aligned}
T_{L2} &= \frac{1}{\pi} \left(\int_{\frac{\pi}{2}}^{\frac{3\pi}{2}} \rho(0.5)(W)^2 A. CL2. (R \sin(x)) dx \right) \\
&= \frac{1}{\pi} \left(\int_{\frac{\pi}{2}}^{\frac{3\pi}{2}} 998.2(0.5)(U + (-\omega R))^2 (H)(c)(1.745 \sin(2.417x))(0.3 \sin(x)) dx \right) \\
&= \frac{1}{\pi} (499.1)(118.244)(0.8)(0.18)(1.745)(0.3) \left(\int_{\frac{\pi}{2}}^{\frac{3\pi}{2}} \sin(2.417x) \sin(x) dx \right) \\
&= (1416.11)(-0.205) \\
&= -290.33 \text{ Nm}
\end{aligned}$$

Sudu 2

$$\begin{aligned}
T_{L1} &= \frac{1}{\pi} \left(\int_{-\frac{\pi}{2}}^{\frac{\pi}{2}} 998.2(0.5)(3 + ((-46.246)(0.3))^2 (H)(c) \left(1.265 \sin \left(2.124 \left(x + \frac{2\pi}{3} \right) \right) \right) (0.3 \sin(x + 2\pi/3)) dx \right) \\
&= (1026.58) \int_{-\frac{\pi}{2}}^{\frac{\pi}{2}} \sin(x + 2\pi/3) \sin(2.124x + 1.416\pi) dx \\
&= (1026.58) (-0.314) \\
&= -322.35 \text{ Nm}
\end{aligned}$$

$$\begin{aligned}
T_{L2} &= \frac{1}{\pi} \left(\int_{\frac{\pi}{2}}^{\frac{3\pi}{2}} 998.2(0.5)(3 + ((-46.246)(0.3))^2(H)(c)(1.745\sin(2.417(x + 2\pi/3)))(0.3 \sin(x + 2\pi/3))dx \right) \\
&= (1416.11) \left(\int_{\frac{\pi}{2}}^{\frac{3\pi}{2}} \sin(2.435x + 1.611\pi)\sin((x+2\pi/3))dx \right) \\
&= (1416.11) (0.3) \\
&= 424.833 \text{ Nm}
\end{aligned}$$

Sudu 3

$$\begin{aligned}
T_{L1} &= \frac{1}{\pi} \left(\int_{-\frac{\pi}{2}}^{\frac{\pi}{2}} 998.2(0.5)(3 + ((-46.246)(0.3))^2(H)(c) \left(1.265\sin \left(2.124(x + \frac{4\pi}{3}) \right) \right) (0.3 \sin(x + 4\pi/3))dx \right) \\
&= (1026.58) \int_{-\frac{\pi}{2}}^{\frac{\pi}{2}} \sin(x+4\pi/3)\sin(2.124x+2.832\pi)dx \\
&= (1026.58) (0.2) \\
&= 205.316 \text{ Nm}
\end{aligned}$$

$$\begin{aligned}
T_{L2} &= \frac{1}{\pi} \left(\int_{\frac{\pi}{2}}^{\frac{3\pi}{2}} 998.2(0.5)(3 + ((-56.897)(0.3))^2(H)(c)(1.745\sin(2.417(x + 4\pi/3)))(0.3 \sin(x + 4\pi/3))dx \right) \\
&= (1416.11) \left(\int_{\frac{\pi}{2}}^{\frac{3\pi}{2}} \sin(2.417x + 3.223\pi)\sin((x+4\pi/3))dx \right) \\
&= (1416.11) (-0.089) \\
&= -126.04 \text{ Nm}
\end{aligned}$$

$$\begin{aligned}
T_L \text{ total} &= ((T_{L1sudu1} + T_{L2sudu1}) + (T_{L1sudu2} + T_{L2sudu2}) + (T_{L1sudu3} + T_{L2sudu3}))/2 \\
&= \frac{(1217.52 - 290.33) + (-322.35 + 424.833) + (205.316 - 126.04)}{2} \\
&= 554.474 \text{ Nm}
\end{aligned}$$

Torsi Drag

Sudu 1

$$\begin{aligned}T_D &= \frac{1}{2\pi} \int_0^{2\pi} \rho(0.5)(W)^2 A. CD. (R \cos(x)) dx \\ &= \frac{1}{2\pi} \int_0^{2\pi} (998.2)(0.5)(3 + (-46.246)(0.3))^2 (H)(c)(1.171 \sin(0.2409x + 1.571) + 1.157 \sin(4.639x - 1.571))(0.3 \cos(x)) dx \\ &= \frac{1}{2\pi} (998.2)(0.5)(118.244)(0.8)(0.18)(0.3) \int_0^{2\pi} ((1.171 \sin(0.2409x + 1.571) + 1.157 \sin(4.639x - 1.571))(\cos(x))) dx \\ &= (405.967) \int_0^{2\pi} 1.171 \sin(0.2409x + 1.571) (\cos(x)) + (1.157 \sin(4.639x - 1.571)) (\cos(x)) dx \\ &= (405.967) \int_0^{2\pi} \frac{1}{2} 1.171 ((\sin(1.2409x + 1.571) + \sin(-0.7591x + 1.571))) dx + \int_0^{2\pi} \frac{1}{2} 1.157 ((\sin(3.639x - 1.571) + \sin(5.639x - 1.571))) dx \\ &= (405.967)(0.151) \\ &= 61.301 Nm\end{aligned}$$

Sudu 2

$$\begin{aligned}T_D &= \frac{1}{2\pi} \int_0^{2\pi} \rho(0.5)(W)^2 A (1.171 \sin(0.2409(x + \frac{2\pi}{3}) + 1.571) + 1.157 \sin(4.639(x + \frac{2\pi}{3}) - 1.571)) (0.3 \cos((x + \frac{2\pi}{3}))) dx \\ &= 405.967 \int_0^{2\pi} (1.171 \sin(0.2409x + 0.167\pi) + 1.157 \sin(4.639x + 3.086\pi)) \cos(x + \frac{2\pi}{3}) dx\end{aligned}$$

$$\begin{aligned}
&= 405.967 \int_0^{2\pi} 1.171(\sin(0.2409x + 0.167\pi)\cos\left(x + \frac{2\pi}{3}\right) + 1.157\sin(4.639x + 3.086\pi)\cos\left(x + \frac{2\pi}{3}\right))dx \\
&= 405.967 \int_0^{2\pi} \frac{1}{2} 1.171((\sin(1.2409x + 0.833\pi) + (\sin(-0.75x - 0.499\pi)))dx + \int_0^{2\pi} \frac{1}{2} 1.157((\sin(3.639x + 2.42\pi) + (\sin(5.639x + 3.752\pi)))dx \\
&= (405.967)(0.751) \\
&= 304.881 \text{ Nm}
\end{aligned}$$

Sudu 3

$$\begin{aligned}
T_D &= \frac{1}{2\pi} \int_0^{2\pi} \rho(0.5)(W)^2 A (1.171\sin\left(0.2409\left(x + \frac{4\pi}{3}\right) + 1.571\right) + 1.157\sin\left(4.639\left(x + \frac{4\pi}{3}\right) - 1.571\right)) \left(0.3 \cos\left(\left(x + \frac{4\pi}{3}\right)\right)\right) dx \\
&= 405.967 \int_0^{2\pi} (1.171 \sin(0.2409x + 0.327\pi) + 1.157\sin(4.639x + 6.179\pi)\cos\left(x + \frac{4\pi}{3}\right))dx \\
&= 405.967 \int_0^{2\pi} 1.171(\sin(0.2409x + 0.327\pi)\cos\left(x + \frac{4\pi}{3}\right) + 1.157\sin(4.639x + 6.179\pi)\cos\left(x + \frac{4\pi}{3}\right))dx \\
&= 405.967 \int_0^{2\pi} \frac{1}{2} 1.171((\sin(1.2409x + 1.66\pi) + (\sin(-0.75x - 1.006\pi)))dx + \int_0^{2\pi} \frac{1}{2} 1.157((\sin(3.639x + 4.846\pi) + (\sin(5.639x + 7.512\pi)))dx \\
&= (405.967)(0.385) \\
&= 156.297 \text{ Nm}
\end{aligned}$$

$$\begin{aligned}T_D \text{ total} &= (T_{Dsudu1} + T_{Dsudu2} + T_{Dsudu3}) \\&= 61.301 + 304.881 + 156.297 \\&= 522.479 \text{ Nm}\end{aligned}$$

$$\begin{aligned}T_{TOTAL} &= (T_{Ltotal} + T_{Dtotal}) \\&= (554.4745) - (522.479) \\&= 31.996 \text{ Nm}\end{aligned}$$

Kecepatan 3.5 m/s

Dik:

$$U = 3.5 \text{ m/s}$$

$$\omega = 54.755 \text{ rad/s}$$

$$C_{L1} = 1.277 \sin(2.093x)$$

$$H = 0.8 \text{ m}$$

$$\rho = 998.2 \text{ kg/m}^3$$

$$C_{L2} = 1.698 \sin(2.421x)$$

$$c = 0.18 \text{ m}$$

$$R = 0.3 \text{ m}$$

$$C_D = 1.173 \sin(0.358x+1.571) + 1.159 \sin(4.522x-1.571)$$

Torsi Lift

Sudu 1

$$T_{L1} = \frac{1}{\pi} \left(\int_{-\frac{\pi}{2}}^{\frac{\pi}{2}} \rho (0.5) (W)^2 A \cdot C_{L1} \cdot (R \sin(x)) dx \right)$$

$$= \frac{1}{\pi} \left(\int_{-\frac{\pi}{2}}^{\frac{\pi}{2}} 998.2 (0.5) (U + (-\omega R))^2 (H) (c) (1.277 \sin(2.093x)) (0.3 \sin(x)) dx \right)$$

$$= \frac{1}{\pi} \left(\int_{-\frac{\pi}{2}}^{\frac{\pi}{2}} 998.2 (0.5) (3.5 + (-54.755)(0.3))^2 (0.8) (0.18) (1.277 \sin(2.093x)) (0.3 \sin(x)) dx \right)$$

$$= \frac{1}{\pi} \cdot 998.2 (0.5) (3.5 + (-54.755)(0.3))^2 (0.8) (0.18) (1.277) (0.3) c \int_{-\frac{\pi}{2}}^{\frac{\pi}{2}} \sin(x) \sin(2.093x) dx$$

$$= \frac{1}{\pi} (499.1) (167.107) (0.8) (0.18) (1.277) (0.3) \int_{-\frac{\pi}{2}}^{\frac{\pi}{2}} \sin(x) \sin(2.093x) dx$$

$$= (1464.56)(1.2)$$

$$= 1757.47 \text{ Nm}$$

$$T_{L2} = \frac{1}{\pi} \left(\int_{\frac{\pi}{2}}^{\frac{3\pi}{2}} \rho(0.5)(W)^2 A. CL2. (R \sin(x)) dx \right)$$

$$= \frac{1}{\pi} \left(\int_{\frac{\pi}{2}}^{\frac{3\pi}{2}} 998.2(0.5)(U + (-\omega R))^2 (H)(c)(1.698 \sin(2.421x))(0.3 \sin(x)) dx \right)$$

$$= \frac{1}{\pi} (499.1)(167.107)(0.8)(0.18)(1.698)(0.3) \left(\int_{\frac{\pi}{2}}^{\frac{3\pi}{2}} \sin(2.421x) \sin(x) dx \right)$$

$$= (1947.39) (-0.194)$$

$$= -377.8 \text{ Nm}$$

Sudu 2

$$T_{L1} = \frac{1}{\pi} \left(\int_{-\frac{\pi}{2}}^{\frac{\pi}{2}} 998.2(0.5)(3.5 + ((-54.755)(0.3))^2 (H)(c) \left(1.277 \sin \left(2.093 \left(x + \frac{2\pi}{3} \right) \right) \right) (0.3 \sin(x + 2\pi/3)) dx \right)$$

$$= (1464.56)(-0.283)$$

$$= -414.5 \text{ Nm}$$

$$\begin{aligned}
T_{L2} &= \frac{1}{\pi} \left(\int_{\frac{\pi}{2}}^{\frac{3\pi}{2}} 998.2(0.5)(3.5 + ((-54.755)(0.3))^2(H)(c)(1.698\sin(2.421(x + 2\pi/3)))(0.3 \sin(x + 2\pi/3))dx \right) \\
&= (1947.39) \left(\int_{\frac{\pi}{2}}^{\frac{3\pi}{2}} \sin(2.421x + 1.614\pi)\sin((x+2\pi/3))dx \right) \\
&= (1947.39) (0.35) \\
&= 681.5 \text{ Nm}
\end{aligned}$$

Sudu 3

$$\begin{aligned}
T_{L1} &= \frac{1}{\pi} \left(\int_{-\frac{\pi}{2}}^{\frac{\pi}{2}} 998.2(0.5)(3.5 + ((-54.755)(0.3))^2(0.8)(0.18) \left(1.277\sin\left(2.093\left(x + \frac{4\pi}{3}\right)\right) \right) (0.3 \sin(x + 4\pi/3))dx \right) \\
&= (1464.56) \int_{-\frac{\pi}{2}}^{\frac{\pi}{2}} \sin(x+4\pi/3)\sin(2.093x+2.790\pi)dx \\
&= (1464.56)(0.173) \\
&= 253.36 \text{ Nm}
\end{aligned}$$

$$\begin{aligned}
T_{L2} &= \frac{1}{\pi} \left(\int_{\frac{\pi}{2}}^{\frac{3\pi}{2}} 998.2(0.5)(3.5 + ((-54.755)(0.3))^2(0.8)(0.18)(1.698 \sin(2.421(x + 4\pi/3)))(0.3 \sin(x + 4\pi/3)) dx \right) \\
&= (1947.39) \left(\int_{\frac{\pi}{2}}^{\frac{3\pi}{2}} \sin(2.421x + 3.228\pi) \sin((x+4\pi/3)) dx \right) \\
&= (1947.39)(-0.074) \\
&= -144.11 \text{ Nm}
\end{aligned}$$

$$\begin{aligned}
T_L \text{ total} &= ((T_{L1sudu1} + T_{L2sudu1}) + (T_{L1sudu2} + T_{L2sudu2}) + (T_{L1sudu3} + T_{L2sudu3}))/2 \\
&= \frac{(1757.47 - 377.8) + (-414.5 + 681.5) + (253.36 - 144.11)}{2} \\
&= 877.96 \text{ Nm}
\end{aligned}$$

Torsi Drag

Sudu 1

$$\begin{aligned}T_D &= \frac{1}{2\pi} \int_0^{2\pi} \rho(0.5)(W)^2 A. CD. (R \cos(x)) dx dx \\&= \frac{1}{2\pi} \int_0^{2\pi} (998.2)(0.5)(3.5 + ((-54.755)(0.3))^2)(0.8)(0.18)(1.173 \sin(0.358x + 1.571) + 1.159 \sin(4.522x - 1.571))(0.3 \cos(x)) dx \\&= \frac{1}{2\pi} (998.2)(0.5)(167.107)(0.8)(0.18)(0.3) \int_0^{2\pi} ((1.173 \sin(0.358x + 1.571) + 1.159 \sin(4.522x - 1.571))(\cos(x))) dx \\&= (573.438) \int_0^{2\pi} 1.173 \sin(0.358x + 1.571) (\cos(x)) + (1.159 \sin(4.522x - 1.571))(\cos(x)) dx \\&= (573.438) \int_0^{2\pi} \frac{1}{2} 1.173 ((\sin(1.358x + 1.571) + (\sin(-0.642x + 1.571))) dx + \int_0^{2\pi} \frac{1}{2} 1.159 ((\sin(3.522x - 1.571) + (\sin(5.522x - 1.571))) dx \\&= (573.438)(-0.254) \\&= -145.653\end{aligned}$$

Sudu 2

$$\begin{aligned}T_D &= \frac{1}{2\pi} \int_0^{2\pi} (998.2)(0.5)(167.107)(0.8)(0.18)(1.173 \sin(0.358(x + \frac{2\pi}{3}) + 1.571) + 1.159 \sin(4.522(x + \frac{2\pi}{3}) - 1.571)) (0.3 \cos(x + \frac{2\pi}{3})) dx \\&= 573.438 \int_0^{2\pi} (1.173 \sin(0.358(x + \frac{2\pi}{3}) + 1.571) + 1.159 \sin(4.522(x + \frac{2\pi}{3}) - 1.571)) \cos(x + \frac{2\pi}{3}) dx\end{aligned}$$

$$\begin{aligned}
&= 573.438 \int_0^{2\pi} 1.173(\sin(0.358x + 0.245\pi)\cos\left(x + \frac{2\pi}{3}\right) + 1.159 \sin(4.522x + 3.008\pi)\cos\left(x + \frac{2\pi}{3}\right))dx \\
&= 573.438 \int_0^{2\pi} \frac{1}{2} 1.173((\sin(1.358x + 0.912\pi) + \sin(-0.642x - 0.421\pi))dx + \int_0^{2\pi} \frac{1}{2} 1.159 ((\sin(3.522x + 2.34\pi) + \sin(5.522x + 3.674\pi))dx \\
&= (573.438)(-0.003) \\
&= -1.72 \text{ Nm}
\end{aligned}$$

Sudu 3

$$\begin{aligned}
T_D &= \frac{1}{2\pi} \int_0^{2\pi} (998.2)(0.5)(167.107)(H)(c)(1.173\sin\left(0.358\left(x + \frac{4\pi}{3}\right) + 1.571\right) + 1.159\sin\left(4.522\left(x + \frac{4\pi}{3}\right) - 1.571\right))\left(0.3 \cos\left(x + \frac{4\pi}{3}\right)\right) dx \\
&= 573.438 \int_0^{2\pi} (1.173\sin\left(0.358\left(x + \frac{4\pi}{3}\right) + 1.571\right) + 1.159 \sin\left(4.522\left(x + \frac{4\pi}{3}\right) - 1.571\right))\cos\left(x + \frac{4\pi}{3}\right)dx \\
&= 573.438 \int_0^{2\pi} 1.173(\sin(0.358x + 0.484\pi)\cos\left(x + \frac{4\pi}{3}\right) + 1.159 \sin(4.522x + 6.029\pi)\cos\left(x + \frac{4\pi}{3}\right))dx \\
&= 573.438 \int_0^{2\pi} \frac{1}{2} 1.173((\sin(1.358x + 1.817\pi) + \sin(-0.642x - 0.849\pi))dx + \int_0^{2\pi} \frac{1}{2} 1.159 ((\sin(3.522x + 4.696\pi) + \sin(5.522x + 7.362\pi))dx \\
&= (573.438)(1.729) \\
&= 991.474 \text{ Nm}
\end{aligned}$$

$$\begin{aligned}T_D \text{ total} &= (T_{Dsudu1} + T_{Dsudu2} + T_{Dsudu3}) \\&= -145.653 - 1.72 + 991.474 \\&= 844.101 \text{ Nm}\end{aligned}$$

$$\begin{aligned}T_{TOTAL} &= (T_{Ltotal} + T_{Dtotal}) \\&= (877.96) - (844.101) \\&= 33.859 \text{ Nm}\end{aligned}$$

Kecepatan 4 m/s

Dik:

$$U = 4 \text{ m/s}$$

$$\omega = -63.263 \text{ rad/s}$$

$$C_{L1} = 1.102 \sin(2.27x)$$

$$H = 0.8636 \text{ m}$$

$$\rho = 998.2 \text{ kg/m}^3$$

$$C_{L2} = 1.683 \sin(2.432x)$$

$$c = 0.1778 \text{ m}$$

$$R = 0.3 \text{ m}$$

$$C_D = 1.161\sin(0.27x+1.571) + 1.136\sin(4.1x-1.571)$$

Torsi Lift

Sudu 1

$$T_{L1} = \frac{1}{\pi} \left(\int_{-\frac{\pi}{2}}^{\frac{\pi}{2}} \rho(0.5)(W)^2 A. CL1. (R \sin(x)) dx \right)$$

$$= \frac{1}{\pi} \left(\int_{-\frac{\pi}{2}}^{\frac{\pi}{2}} 998.2(0.5)(U + (-\omega R))^2 (H)(c)(1.102 \sin(2.27x))(0.3 \sin(x)) dx \right)$$

$$= \frac{1}{\pi} \left(\int_{-\frac{\pi}{2}}^{\frac{\pi}{2}} 998.2(0.5)(4 + ((-63.263)(0.3))^2(0.8)(0.18)(1.102 \sin(2.27x))(0.3 \sin(x)) dx \right)$$

$$= \frac{1}{\pi} \cdot 998.2(0.5)(4 + ((-63.263)(0.3))^2(0.8)(0.18)(1.102)(0.3) \int_{-\frac{\pi}{2}}^{\frac{\pi}{2}} \sin(x) \sin(2.27x) dx$$

$$= \frac{1}{\pi} (499.1)(233.57)(0.8)(0.18)(1.102)(0.3) \int_{-\frac{\pi}{2}}^{\frac{\pi}{2}} \sin(x) \sin(2.27x) dx$$

$$= (1766.526)(0.99)$$

$$= 1748.86 \text{ Nm}$$

$$T_{L2} = \frac{1}{\pi} \left(\int_{\frac{\pi}{2}}^{\frac{3\pi}{2}} \rho(0.5)(W)^2 A. CL2. (R \sin(x)) dx \right)$$

$$= \frac{1}{\pi} \left(\int_{\frac{\pi}{2}}^{\frac{3\pi}{2}} 998.2(0.5)(U + (-\omega R))^2 (H)(c)(1.683 \sin(2.432x)) (0.3 \sin(x)) dx \right)$$

$$= \frac{1}{\pi} (499.1)(233.57)(0.8)(0.18)(1.683)(0.3) \left(\int_{\frac{\pi}{2}}^{\frac{3\pi}{2}} \sin(2.432x) \sin(x) dx \right)$$

$$= (2697.88)(-0.164)$$

$$= -442.453 \text{ Nm}$$

Sudu 2

$$T_{L1} = \frac{1}{2\pi} \left(\int_{-\frac{\pi}{2}}^{\frac{\pi}{2}} 998.2(0.5)(4 + ((-95.203)(0.3))^2)(0.8)(0.18) \left(1.102 \sin\left(2.27\left(x + \frac{2\pi}{3}\right)\right) \right) (0.3 \sin(x + 2\pi/3)) dx \right)$$

$$= (1766.526)(-0.6)$$

$$= -1059.92 \text{ Nm}$$

$$\begin{aligned}
T_{L2} &= \frac{1}{2\pi} \left(\int_{\frac{\pi}{2}}^{\frac{3\pi}{2}} 998.2(0.5)(4 + ((-95.203)(0.3))^2(0.8)(0.18)(1.683\sin(2.432(x + 2\pi/3)))(0.3\sin(x + 2\pi/3))dx \right) \\
&= (2697.88) \left(\int_{\frac{\pi}{2}}^{\frac{3\pi}{2}} \sin(2.432x + 1.621\pi)\sin((x+2\pi/3))dx \right) \\
&= (2697.88)(0.33) \\
&= 890.3 \text{ Nm}
\end{aligned}$$

Sudu 3

$$\begin{aligned}
T_{L1} &= \frac{1}{2\pi} \left(\int_{-\frac{\pi}{2}}^{\frac{\pi}{2}} 998.2(0.5)(4 + ((-95.203)(0.3))^2(0.8)(0.18) \left(1.102 \sin \left(2.27 \left(x + \frac{4\pi}{3} \right) \right) \right) (0.3 \sin(x + 4\pi/3)) dx \right) \\
&= (1766.526) \int_{-\frac{\pi}{2}}^{\frac{\pi}{2}} \sin(x+4\pi/3)\sin(2.27x+3.026\pi)dx \\
&= (1766.526)(0.52) \\
&= 918.5 \text{ Nm}
\end{aligned}$$

$$\begin{aligned}
T_{L2} &= \frac{1}{2\pi} \left(\int_{\frac{\pi}{2}}^{\frac{3\pi}{2}} 998.2(0.5)(4 + ((-95.203)(0.3))^2(0.8)(0.18)(1.683 \sin(2.432(x + 4\pi/3)))(0.3 \sin(x + 4\pi/3)) dx \right) \\
&= (2697.88) \left(\int_{\frac{\pi}{2}}^{\frac{3\pi}{2}} \sin(2.432x + 3.242\pi) \sin((x+4\pi/3)) dx \right) \\
&= (2697.88)(-0.034) \\
&= -91.728 \text{ Nm}
\end{aligned}$$

$$\begin{aligned}
T_L \text{ total} &= (T_{L1sudu1} + T_{L2sudu1}) + (T_{L1sudu2} + T_{L2sudu2}) + (T_{L1sudu3} + T_{L2sudu3}) \\
&= \frac{(1748.86 - 442.453) + (-1059.92 + 890.3) + (918.5 - 91.728)}{2} \\
&= 981.779 \text{ Nm}
\end{aligned}$$

Torsi Drag

Sudu 1

$$T_D = \frac{1}{2\pi} \int_0^{2\pi} \rho(0.5)(W)^2 A. CD. (R \cos(x)) dx dx$$

$$T_D = \frac{1}{2\pi} \int_0^{2\pi} (998.2)(0.5)(4 + ((-63.263)(0.3))^2(0.8)(0.18) (1.161\sin(0.27x + 1.571) + 1.136\sin(4.1x - 1.571))(0.3 \cos(x)) dx$$

$$\begin{aligned} T_D &= \frac{1}{2\pi} (998.2)(0.5)(233.57)(0.8)(0.18)(0.3) \int_0^{2\pi} (1.161\sin(0.27x + 1.571) + 1.136\sin(4.1x - 1.571))(\cos(x)) dx \\ &= (801.509) \int_0^{2\pi} (1.161\sin(0.27x + 1.571)(\cos(x)) + 1.136\sin(4.1x - 1.571))(\cos(x)) dx \\ &= (801.509) \int_0^{2\pi} \frac{1}{2} 1.161((\sin(1.27x + 1.571) + \sin(-0.73x + 1.571))) dx + \int_0^{2\pi} \frac{1}{2} 1.136((\sin(3.1x - 1.571) + \sin(5.1x - 1.571))) dx \\ &= (801.509) \int_0^{2\pi} \frac{1}{2} 1.161((\sin(1.27x + 0.00643\pi) + \sin(-0.73x + 0.00643\pi))) dx + \int_0^{2\pi} \frac{1}{2} 1.136((\sin(3.1x - 0.00643\pi) + \sin(5.1x - 0.00643\pi))) dx \\ &= (801.509)(-0.334) \\ &= -267.704 Nm \end{aligned}$$

Sudu 2

$$\begin{aligned} T_D &= \frac{1}{2\pi} \int_0^{2\pi} (998.2)(0.5)(4 + ((-63.263)(0.3))^2(H)(c) (1.161\sin\left(0.27\left(x + \frac{2\pi}{3}\right) + 1.571\right) + 1.136\sin\left(4.1\left(x + \frac{2\pi}{3}\right) - 1.571\right))\left(0.3 \cos\left(\left(x + \frac{2\pi}{3}\right)\right)\right) dx \\ &= (801.509) \int_0^{2\pi} (1.161 \sin(0.27x + 0.18\pi) + 1.136\sin(4.1x + 2.73\pi))\cos\left(x + \frac{2\pi}{3}\right) dx \end{aligned}$$

$$\begin{aligned}
&= (801.509) \int_0^{2\pi} 1.161(\sin(0.27x + 0.18\pi)\cos(x + \frac{2\pi}{3}) + 1.136\sin(4.1x + 2.73\pi)\cos(x + \frac{2\pi}{3}))dx \\
&= (801.509) \int_0^{2\pi} \frac{1}{2} 1.161((\sin(1.27x + 0.84\pi) + (\sin(-0.73x - 0.48\pi)))dx + \int_0^{2\pi} \frac{1}{2} 1.136((\sin(3.1x + 2.07\pi) + (\sin(5.1x + 3.39\pi)))dx \\
&= (801.509) (0.488) \\
&= 391.136 \text{ Nm}
\end{aligned}$$

Sudu 3

$$\begin{aligned}
T_D &= \frac{1}{2\pi} \int_0^{2\pi} (998.2)(0.5)(4 + ((-63.263)(0.3))^2(H)(c)(1.161\sin(0.27(x + \frac{4\pi}{3}) + 1.571) + 1.136\sin(4.1(x + \frac{4\pi}{3}) - 1.571)) (0.3 \cos(x + \frac{4\pi}{3})) dx \\
&= (801.509) \int_0^{2\pi} (1.161 \sin(0.27x + 0.366\pi) + 1.136\sin(4.1x + 5.46\pi)\cos(x + \frac{4\pi}{3}))dx \\
&= (801.509) \int_0^{2\pi} (1.161 \sin(0.27x + 0.366\pi)\cos(x + \frac{4\pi}{3}) + (1.136\sin(4.1x + 5.46\pi)\cos(x + \frac{4\pi}{3}))dx \\
&= (801.509) \int_0^{2\pi} \frac{1}{2} 1.161((\sin(1.27x + 1.699\pi) + (\sin(-0.73x - 0.964\pi)))dx + \int_0^{2\pi} \frac{1}{2} 1.136((\sin(3.1x + 4.13\pi) + (\sin(5.1x + 6.79\pi)))dx \\
&= (801.509) (1.01) \\
&= 809.524 \text{ Nm}
\end{aligned}$$

$$\begin{aligned}T_D \text{ total} &= (T_{Dsudu1} + T_{Dsudu2} + T_{Dsudu3}) \\&= -267.704 + 391.136 + 809.524 \\&= 932.956 \text{ Nm}\end{aligned}$$

$$\begin{aligned}T_{TOTAL} &= (T_{Ltotal} + T_{Dtotal}) \\&= (981.779) - (932.956) \\&= 48.823 \text{ Nm}\end{aligned}$$

2.2 Perhitungan Daya Turbin

Rumus: $P_t = T \cdot \omega$

$U = 2 \text{ m/s} \quad \omega = 29.23 \text{ Rad/s} \quad T = 12.084 \text{ Nm}$

$P_t = T \cdot \omega$

$P_t = 12.084 \cdot 29.23$

$P_t = 353.215 \text{ Watt}$

$U = 2.5 \text{ m/s} \quad \omega = 37.738 \text{ Rad/s} \quad T = 24.05 \text{ Nm}$

$P_t = T \cdot \omega$

$P_t = 24.05 \cdot 37.738$

$P_t = 907.6 \text{ Watt}$

$U = 3 \text{ m/s} \quad \omega = 46.246 \text{ Rad/s} \quad T = 31.996 \text{ Nm}$

$P_t = T \cdot \omega$

$P_t = 31.996 \cdot 46.246$

$P_t = 1479.687 \text{ Watt}$

$U = 3.5 \text{ m/s} \quad \omega = 54.755 \text{ Rad/s} \quad T = 33.859 \text{ Nm}$

$P_t = T \cdot \omega$

$P_t = 33.859 \cdot 54.755$

$P_t = 1853.95 \text{ Watt}$

$U = 4 \text{ m/s} \quad \omega = 63.263 \text{ Rad/s} \quad T = 48.823 \text{ Nm}$

$P_t = T \cdot \omega$

$P_t = 48.823 \cdot 63.263$

$P_t = 3088.689 \text{ Watt}$

2.3 Perhitungan Daya Hidrolis

$$\begin{aligned} \text{Rumus : } P_h &= \rho g Q H \\ &= \rho g (A U) \left(\frac{U^2}{2g} \right) \\ &= \rho (A) \left(\frac{U^3}{2} \right) \\ &= \rho (H)(D) \left(\frac{U^3}{2} \right) \end{aligned}$$

$$U = 2 \text{ m/s} \quad H = 0.8 \text{ m} \quad D = 0.6 \quad \rho = 998.2 \text{ kg/m}^3$$

$$P_h = \rho (H)(D) \left(\frac{U^3}{2} \right)$$

$$P_h = (998.2) (0.8) (0.6) \left(\frac{2^3}{2} \right)$$

$$P_h = 1916.544 \text{ Watt}$$

$$U = 2.5 \text{ m/s} \quad H = 0.8 \text{ m} \quad D = 0.6 \quad \rho = 998.2 \text{ kg/m}^3$$

$$P_h = \rho (H)(D) \left(\frac{U^3}{2} \right)$$

$$P_h = (998.2) (0.8) (0.6) \left(\frac{2.5^3}{2} \right)$$

$$P_h = 3743.25 \text{ Watt}$$

$$U = 3 \text{ m/s} \quad H = 0.8 \text{ m} \quad D = 0.6 \quad \rho = 998.2 \text{ kg/m}^3$$

$$P_h = \rho (H)(D) \left(\frac{U^3}{2} \right)$$

$$P_h = (998.2) (0.8) (0.6) \left(\frac{3^3}{2} \right)$$

$$P_h = 6468.336 \text{ Watt}$$

$$U = 3.5 \text{ m/s} \quad H = 0.8 \text{ m} \quad D = 0.6 \quad \rho = 998.2 \text{ kg/m}^3$$

$$P_h = \rho (H)(D) \left(\frac{U^3}{2} \right)$$

$$P_h = (998.2) (0.8) (0.6) \left(\frac{3.5^3}{2} \right)$$

$$P_h = 10271.478 \text{ Watt}$$

$$U = 4 \text{ m/s} \quad H = 0.8 \text{ m} \quad D = 0.6 \quad \rho = 998.2 \text{ kg/m}^3$$

$$P_h = \rho (H)(D) \left(\frac{U^3}{2} \right)$$

$$P_h = (998.2) (0.8) (0.6) \left(\frac{4^3}{2} \right)$$

$$P_h = 15332.352 \text{ Watt}$$

2.4 Perhitungan Efisiensi Turbin (ηT)

$$\text{Rumus : } \eta T = \frac{P_t}{P_h} \times 100\%$$

1. Kecepatan aliran 2 m/s

$$P_T = 353.215 \text{ Watt} \quad P_H = 1916.544 \text{ Watt}$$

$$\eta T = \frac{P_t}{P_h} \times 100\%$$

$$\eta T = \frac{353.215 \text{ Watt}}{1916.544 \text{ Watt}} \times 100\%$$

$$\eta T = 18.4 \%$$

2. Kecepatan aliran 2.5 m/s

$$P_T = 1658.396 \text{ Watt} \quad P_H = 3743.25 \text{ Watt}$$

$$\eta T = \frac{P_t}{P_h} \times 100\%$$

$$\eta T = \frac{907.6 \text{ Watt}}{3743.25 \text{ Watt}} \times 100\%$$

$$\eta T = 24.2 \%$$

3. Kecepatan aliran 3 m/s

$$P_T = 2931.904 \text{ Watt} \quad P_H = 6468.336 \text{ Watt}$$

$$\eta T = \frac{P_t}{P_h} \times 100\%$$

$$\eta T = \frac{1479.687 \text{ Watt}}{6468.336 \text{ Watt}} \times 100\%$$

$$\eta T = 22.9 \%$$

4. Kecepatan aliran 3.5 m/s

$$P_T = 3566.795 \text{ Watt} \quad P_H = 10271.478 \text{ Watt}$$

$$\eta T = \frac{P_t}{P_h} \times 100\%$$

$$\eta T = \frac{1853.95 \text{ Watt}}{10271.478 \text{ Watt}} \times 100\%$$

$$\eta T = 18.049 \%$$

5. Kecepatan aliran 4 m/s

$$P_T = 5530.198 \text{ Watt} \quad P_H = 15332.352 \text{ Watt}$$

$$\eta T = \frac{P_t}{P_h} \times 100\%$$

$$\eta T = \frac{3088.689 \text{ Watt}}{15332.352 \text{ Watt}} \times 100\%$$

$$\eta T = 20.145 \%$$