Prediction of Sliding Wear of Artificial Rough Surfaces

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Abstract:
When two surfaces are brought in contact, deformation takes place at asperity level. The local pressure distribution and deformation of the contacting surfaces are important with respect to wear. This paper describes a wear model to predict the wear of rough sliding contacts. The wear model is based on the general Archard’s wear equation in combination with finite element analysis (FEA). In this paper the roughness is represented by uniformly distributed spherical asperities. The proposed model, FE in combination with Archard’s wear law, has proven to be a powerful tool in predicting wear of rough surfaces.

Keywords: FEA, Rough Surface, Sliding Contact, Wear

1. Introduction

All surfaces, manufactured or natural, are not perfectly smooth. Roughness represents the deviation from a perfectly smooth surface and is a composition of peaks and valleys, called asperities. Roughness can also be considered as a summation of wavy surface, on micro scale, with their height being 2-5% of the wavelength [1]. Experiments and analytical studies indicate that the real area of contact between solid surfaces, for instance metals and ceramics, occur at isolated points and the real contact area is a very small portion of the apparent area for flat surfaces (conformal contacts) or curved surfaces (concentrated contacts).

The surface model used for a rough engineering surface often used in contact modeling is based on the Greenwood and Williamson’s model [2]. A rough surface is represented by identical, uniformly distributed spherical asperities, and differing only in their heights above a reference plane. The reference plane of the asperities is not identical to the mean plane of the surface heights. It is located, rather, above the mean plane of the height distribution by an order of the standard deviation of the profile [3]. Other models that are based on the Greenwood and Williamson model can be found in [4-7]. In most of these contact models, the asperities are assumed to be hemispherical or paraboloidal and the local contact stresses can be calculated using the Hertz solution [8].

Holm [9] and Archard [10] were the pioneers in developing the sliding wear model. Archard’s wear equation postulates that the wear rate is defined by the volume worn away per unit sliding distance and the load. The wear depth of wear can be calculated on the basis of the wear rate, sliding distance and contact pressure.

\[
\Delta h = \frac{\Delta V}{F \cdot s} = \frac{k_D \Delta h}{p \Delta s} \tag{1}
\]

in which \(k_D\) is the wear rate, \(\Delta V\) is the wear volume, \(F\) the normal load, \(s\) the sliding distance, \(\Delta s\) incremental sliding distance, \(\Delta h\) the wear depth and \(p\) the contact pressure.

The change in geometry of the surface is mainly determined by the contact pressure distribution and the (local) deformation of the solid surfaces. The procedure to calculate the pressure distribution and deformation is based on discretizing the continuum equations, finite element analysis (FEA). The advantages of a 3D model are the utilization of the correct geometry (surface topography, dimensions, and degrees of freedom) and the ability to compute stresses and deformations in the entire body. Due to the very fine meshing, however, a 3D model require high processing times. This is a disadvantage when regarding extensive parameter studies and
optimizations. Thus, FEA seems not a practical choice for computing the real contact between rough surfaces [11].

Despite the above mentioned disadvantage investigators use FEA to understand the phenomena related to wear and build their models. The models developed in [12-15] are based on real surface roughness. The main result of these investigations is that the complex analytical stress-deformation expressions are converted to a system of linear algebraic equations which are generally solved, based on iterative numerical methods. This technique takes into account the interaction of deformation from all contact points (which is not the case in the Greenwood and Williams contact model) and predicts the real contact area of rough surfaces under loading. It presents useful information on the distribution of contact pressure, number of contacts, area of contact, and the spacing between the contacts.

There are many papers presented on wear modeling using Archard's wear equation. Podra [16] presented the sliding wear of a pin-on-disc system. He performed wear simulations with FEA commercial software ANSYS to determine the contact pressure distribution and applied Archard's wear relation to calculate the wear as a function of the sliding distance. His work was further developed by Andersson and co-workers [17-20]. A numerical simulation of the wear of a cylindrical steel roller oscillating against a flat steel surface was performed by Oqvist [21]. The simulation was done with incremental sliding distance steps and the pressure was recalculated as the surface geometry changed.

Recently, Hegadekatte [22-25] proposed a wear modeling scheme similar to Podra [16]. He performed a 3D static contact calculation with the commercial FE code ABAQUS. The wear system considered is a pin-on-disc contact configuration.

2. Finite Element Modeling

In the pin-on-disc system a hemispherical rough pin is sliding against a smooth disc, as depicted in Fig. 1. The wear simulation is performed with the commercial package ABAQUS. The simulation does not aim to simulate the entire sliding process of contact system but instead treats the problem of sliding wear as 'quasi-static' to save the computational expense. In the model of Hegadekatte et al. [25] a pin with radius $R_p$, 0.794 mm is used having asperities with the certain radius. The operational conditions and some properties are given in Table 1 and are similar with [25] except for the radius of the asperities and distance between the asperities.

![Figure 1. Pin-on-disc contact system and its refined mesh in the contact region.](Image)
In the present model the radius of the asperities \( (R_{as}) \) is 50 and 25 µm. The inputs for the simulation, see the flowchart of Fig. 2, are geometry, material model, contact definition and boundary conditions. The first step of this simulation is determining the contact pressure.

**Figure 2.** Flowchart wear simulation.

### Table 1. Operational conditions and some material properties

<table>
<thead>
<tr>
<th>Description</th>
<th>Dimension</th>
</tr>
</thead>
<tbody>
<tr>
<td>Material of pin and disc</td>
<td>Silicon Nitride (Si₃N₄)</td>
</tr>
<tr>
<td>Radius of pin ( (R_p) )</td>
<td>0.794 mm</td>
</tr>
<tr>
<td>Radius of asperities ( (R_{as}) )</td>
<td>50 µm and 25 µm</td>
</tr>
<tr>
<td>Distance between asperities</td>
<td>1° (for 50 µm) and 0.7° (for 25 µm)</td>
</tr>
<tr>
<td>Poisson's ratio ( (\nu) )</td>
<td>0.24</td>
</tr>
<tr>
<td>Contact load ( (F_c) )</td>
<td>200mN</td>
</tr>
<tr>
<td>Wear rate ( (k_w) )</td>
<td>13.5E-9 mm³/Nmm</td>
</tr>
<tr>
<td>Young's Modulus ( (E) )</td>
<td>304 GPa</td>
</tr>
</tbody>
</table>

The local wear depth is computed from a combination of the finite element calculated contact pressure and Archard’s wear model:

\[
\Delta h^w = k_D \cdot p(x, y) \cdot \Delta s
\]  

In which, \( \Delta h^w \) is the wear depth, \( k_D \) the wear rate, \( p(x, y) \) the contact pressure distribution and \( \Delta s \) the incremental sliding distance. The wear of the disc is not taken into account. After this step, the geometry of the
contact system is updated. This is repeated until the set sliding distance is met. For a more detailed FEA process to predict wear in a tribo-system, the reader is referred to [26].

The finite element model was solved using the memory of 4 GB of a personal computer and the computation time was about 15 minutes for a single simulation. Both pin and disc consists of 84159 elements. The element of A4-node linear tetrahedron was selected for this purpose. From Fig. 1b, it is clear that a refined mesh is used in the contact area and outside the contact a coarse grid is used to minimize the computational time.

3. Results and Discussion

The calculated contact area and stresses are shown in Fig. 3. The asperity at the center of the contact is loaded more than the asperities located further away from the center, this due the geometrical setting of the asperities on a curved body. In case of a conformal contact the loading of the asperities is uniform.

![Fig. 3. (a) Real contact area of pin surface on asperity level R_gas 50 μm (b) pressure distribution for the initial contact at the 3rd, 1st, 5th asperity.](image)

The contact pressure distribution on asperity level is presented in Fig. 4. From this figure it becomes clear that as wear increases with the sliding distance the real contact area increases. Further, the pressure distribution across an asperity changes significantly from an initial Hertzian pressure distribution to a pressure distribution showing at the edge of each worn asperity a pressure rise. Due to wear of the asperities located at the center of the macroscopic contact more and more surrounding asperities are involved in carrying the load.

![Figure 4. Contact pressure distribution on asperity level R_gas 50 μm.](image)
The computed wear of the asperities is presented in Fig. 5. As expected the wear of the asperity at the center of contact area is higher than the surrounding asperities. Due to the symmetric artificial rough surface wear of the 2\textsuperscript{nd}, 3\textsuperscript{rd}, 4\textsuperscript{th}, and 5\textsuperscript{th} asperity is the same (see Fig. 5). At the start of the sliding process, the wear, reduction of the asperity height, is high (initial phase) and then tends to stabilize (final phase). In the terms of mechanical systems, the initial and the final phases are called running-in and steady-state respectively [27].

![Figure 5](image5.png)

**Figure 5.** Wear “depth” of the asperities of the silicon nitride (Si\textsubscript{3}N\textsubscript{4}) pin as a function of the sliding distance.

From Fig. 6, it can be concluded that both the average contact pressure as well as the surface roughness ($R_a$) at the initial phase of the sliding process is high and then tend to stabilize in final phase, due to the conformal shape of the asperities.

![Figure 6](image6.png)

(a) Average contact pressure and (b) surface roughness as a function of the sliding distance.

**4. Conclusions**

In this paper, a model in wear prediction of a rough surface sliding contact has been presented. A hemispherical pin, made of silicon nitride Si\textsubscript{3}N\textsubscript{4} with an artificial rough surface represented by uniform distributed spherical asperities is in contact with a smooth flat disc. Both the pin and disc have similar mechanical properties. It can be concluded that the wear of the asperity at the center of the contact of the rough surface is higher than the surrounding asperities. The proposed model, FE in combination with Archard’s wear law, has proven to be a powerful tool in predicting wear of rough surfaces. Future studies will be
conducted on the running-in of components in mechanical systems like MEMS in which artificial surfaces are applied to enhance the tribological performance.

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References