Three-Phase Line Modeling for Unbalance Distribution Power Flow Using Forward-Backward Propagation Algorithm

Agus Ulinuha Department of Electrical Engineering Universitas Muhammadiyah Surakarta Surakarta, Indonesia Email: agus ulinuha@ums.ac.id

Abstract— A direct modeling for three-phase distribution line is employed for unbalance power flow calculation. The effectiveness of the model is demonstrated by the needless of decoupling the system into symmetrical components or individual phases. A suitable method for unbalance power flow analysis may then be used. This paper proposes Forward-Backward Propagation for the power flow. The equivalent injection current method is employed to represent the loads and shunt admittances. The algorithm offers robust and good convergence characteristics for radial distribution system. The algorithm is presented for the IEEE 34-bus system. The unbalance level of the system is also analysed.

Keywords-direct modeling; unbalance power flow analysis, forward-backward propagation, equivalent injection current

I. INTRODUCTION

Power flow calculation is backbone of power system analysis and design. It is essential for analysis of any power system in the operational as well as planning stages. The calculation is initially carried out by formulating the network equation. Node-voltage method, which is the most suitable form for many power system analyses, is commonly used. Mathematically, power flow problem requires solution of simultaneous nonlinear equations and normally employs an iterative method, such as Gauss-Seidel and Newton-Raphson.

Power flow calculation is normally performed by simply considering that the system under study is balance. Hence, the calculation is carried out for single phase assuming that the other two phases are exactly the same but with the 120 degrees phase difference. The asymmetry in lines and loads produces a certain level of unbalance in real power system and this is considered as disturbance whose level should be controlled to maintain the electromagnetic compatibility of the system [1].

For distribution system, in particular, the system is inherently unbalanced, due to factors such as the unbalance of customer loads, the presence of unsymmetrical line spacing, and the combination of single, double and threephase line sections. Therefore, three-phase power flow is necessary to accurately simulate the unbalance system.

Inclusion of unbalance increases the dimension of problem as all the three phases need to be considered instead of single phase balanced representation. On the other hand, distribution system commonly constructed as radial system with high R/X ratio may cause the sophisticated power flow algorithms fail to converge. The robust algorithm for threephase power flow is therefore needed.

In order to simplify the problem, some approaches have been carried out for three-phase power flow problem. Decomposition of the coupled unbalance system into positive, negative and zero symmetrical components is the most popular approach used for the problem [2, 3]. This eliminates the mutual coupling between phases so a threephase power flow can be run three times, once for each phase. However, if the coupling between sequences occurs, then there is no real advantage in decomposing the system into the symmetrical components. Furthermore, this may result in significant error in calculation.

Another approach is decoupling the three-phase system into individual phases by introducing compensation current injections [4-7]. Therefore, a three-phase power flow can be solved independently for every phase without utilization of symmetrical components. All components are modeled by phase voltages, admittances and independent current sources. This approach will work well as long as every component can be modeled in the admittance matrix or can be converted into equivalent injection current.

The methods for three-phase distribution networks can be basically divided into two classes, Gauss-Seidel [4, 8] and Newton-Raphson [5, 9, 10]. Gauss-Seidel method needs much iteration and is known to be slow. Newton-Raphson has good convergence characteristic, but the Jacobian that needs to be partially or totally calculated in every iteration makes this approach unattractive.

This paper presents three-phase power flow for unbalance distribution system using forward-backward propagation technique. The algorithm works directly on the system without any modification. Therefore, there is no need to decompose the system into symmetrical components as well as to decouple the system into individual phases. However, the conversion of load and shunt element into their equivalent injection current is necessary. Distribution line charging is usually too small to be included [5]. The algorithm is implemented on IEEE 34-bus system including asymmetrical lines and unbalance loads. The level of system unbalance is investigated using quantitative voltage unbalance analysis.

II. . SYSTEM MODELLING

A. Line Modelling

The accuracy of three-phase power flow results greatly depends on the line impedance model. Therefore, an exact model of a three-phase line section needs to be firstly developed. The model of distribution line feeder in [11] will be developed and used in this paper. An equivalent circuit for a three-phase line section is shown in Fig. 1.

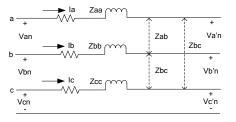


FIGURE 1. THREE-PHASE LINE MODEL

The modelling of three-phase lines starts with determination of self and mutual impedances of a line section which are functions of the conductors and the spacing between conductors on the pole or underground. The "modified" form of Carson's equations [11] are used to determine the self and mutual impedances (Ω /mile) of this model and are given by the following equations:

$$z_{ii} = r_i + 0.0953 + j0.12134 \times \left[\ln(1/GMR_i) + 7.934 \right]$$
(1)

$$z_{ij} = 0.0953 + j0.12134 \times \left[\ln(1/D_{ij}) + 7.934 \right]$$
(2)

Where r_i is the conductor resistance (Ω /mile), GMR_i is the conductor geometric mean radius (ft), and D_{ij} is the spacing between conductors *i* and *j* (ft). Application of (1) and (2) to the three-phase line indicated in Fig. 1 results in a 4×4 "primitive impedance matrix":

$$[Zprim] = \begin{bmatrix} z_{aa} & z_{ab} & z_{ac} & z_{an} \\ z_{ba} & z_{bb} & z_{bc} & z_{bn} \\ z_{ca} & z_{cb} & z_{cc} & z_{cn} \\ z_{na} & z_{nb} & z_{nc} & z_{nn} \end{bmatrix}$$
(3)

By applying Kron reduction [11], this matrix may be reduced into 3×3 "phase impedance matrix" whose elements are determined by the following equation:

$$Z_{ij} = z_{ij} - z_{in} z_{nj} / z_{nn} \tag{4}$$

And the resulted "phase impedance matrix" is:

$$\begin{bmatrix} Z_{abc} \end{bmatrix} = \begin{bmatrix} Z_{aa} & Z_{ab} & Z_{ac} \\ Z_{ba} & Z_{bb} & Z_{bc} \\ Z_{ca} & Z_{cb} & Z_{cc} \end{bmatrix}$$
(5)

B. Load Modelling

The load (balance and unbalance) is represented by its equivalent injection current. The load modeling in [4] is adopted in this paper. For three-phase loads connected in wye or single-phase loads connected line to neutral, the equivalent injection currents at k^{th} bus are determined by the following equation:

$$I_m^k = \frac{P_m^k - jQ_m^k}{V_m^k *}; \ m \in [a, b, c] : \text{phase}$$
(6)

Where P_m , Q_m , V_m^* denote real power, reactive power, and complex conjugate of the voltage phasor for each phase, respectively. For three-phase loads connected in delta or single-phase loads connected line to line, the equivalent injection currents at the k^{th} bus are determined by the following equations:

$$I_{a}^{k} = \frac{P_{ab}^{k} - jQ_{ab}^{k}}{V_{a}^{k} * - V_{b}^{k} *} - \frac{P_{ca}^{k} - jQ_{ca}^{k}}{V_{c}^{k} * - V_{a}^{k} *}$$

$$I_{b}^{k} = \frac{P_{bc}^{k} - jQ_{bc}^{k}}{V_{b}^{k} * - V_{c}^{k} *} - \frac{P_{ab}^{k} - jQ_{ab}^{k}}{V_{a}^{k} * - V_{b}^{k} *}$$

$$I_{c}^{k} = \frac{P_{ca}^{k} - jQ_{ca}^{k}}{V_{c}^{k} * - V_{a}^{k} *} - \frac{P_{bc}^{k} - jQ_{bc}^{k}}{V_{b}^{k} * - V_{c}^{k} *}$$
(7)

Where P_n , Q_n , $n \in [ab, bc, ca]$, represents the real and reactive load connected between the respective phases, and V_m^* , $m \in [a, b, c]$ denotes the complex conjugate of the voltage phasor for each phase, respectively.

C. Shunt Admittance Modelling

Three phase shunt capacitors can also be represented by equivalent injection currents [4]. Assuming that the capacitor bank has an ungrounded wye connection, the current injection in each phase can be expressed by:

$$I_{a}^{sh} = \frac{y^{sh}}{3} \left(-2V_{a}^{k} + V_{b}^{k} + V_{c}^{k} \right)$$

$$I_{b}^{sh} = \frac{y^{sh}}{3} \left(V_{a}^{k} - 2V_{b}^{k} + V_{c}^{k} \right)$$

$$I_{c}^{sh} = \frac{y^{sh}}{3} \left(V_{a}^{k} + V_{b}^{k} - 2V_{c}^{k} \right)$$
(8)

Where $y^{sh} = jQ^0//V^0/^2$; Q^0 is the nominal reactive power per phase and $/V^0/$ is the magnitude of the nominal voltage each phase. If the capacitor bank has a grounded wye connection, then the injection current is:

$$I_{a}^{sh} = -y^{sh}V_{a}^{k}$$

$$I_{b}^{sh} = -y^{sh}V_{b}^{k}$$

$$I_{c}^{sh} = -y^{sh}V_{c}^{k}$$
(9)

III. FORWARD-BACKWARD ALGORITHM

Power flow is calculated by initially mapping the distribution network to determine forward and backward propagation paths followed by branch current calculation and bus voltages calculation.

A. Branch Current Calculation

Following the backward propagation path, branch current can be calculated using the equivalent bus injection currents. The branch current is successively calculated for the network ends toward the source (swing). The voltage at each bus therefore needs to be firstly determined. For the first iteration, the voltage at each bus is set to 1.0 pu with the angle of 0, -120 and 120 degrees for phase a, b, and c, respectively. These voltages are updated during the iteration and therefore the injection currents will also change.

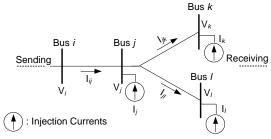


FIGURE 2. PART OF A DISTRIBUTION SYSTEM

Fig. 2 indicates a part of distribution system and bus injection currents. The relationships between branch currents and injection currents are:

$$I_{jk} = -I_k$$

$$I_{jl} = -I_l$$

$$I_{ij} = I_{jk} + I_{jl} - I_k$$
(10)

Where I_{jk} is the branch current between bus *j* and bus *k*, and I_j injection currents at bus, respectively.

B. Bus Voltage Calculation

Following the forward propagation path, the voltage at each bus is calculated using the obtained branch currents and line impedance. The voltages are consecutively calculated from the source (swing) toward the network ends. The voltage of swing bus is kept constant at $1.0 \angle 0^0$ pu, $1.0 \angle -120^0$ pu, and $1.0 \angle 120^0$ pu for phase a, b, and c, respectively. For the part of system indicated in Fig. 2, the bus voltages can be calculated as follows:

$$V_{j} = V_{i} - Z_{ij}I_{ij}$$

$$V_{k} = V_{j} - Z_{jk}I_{jk}$$

$$V_{l} = V_{j} - Z_{jl}I_{jl}$$
(11)

Where V_j is the voltage at bus j and Z_{jk} is the impedance of line section between bus j and k. The updated bus voltages are then used to calculate the bus injection currents. It should

be noted that all calculations are carried in the three-phase frame.

C. Convergence Criteria

The outlined steps for branch currents and bus voltages calculations are invoked during the power flow iteration. The iteration converges if the different of bus voltages for the consecutive iterations is equal to or less than the prescribed tolerance. The voltage mismatch of bus j at the nth iteration is given by:

$$\Delta V_j^n = V_j^n - V_j^{n-1} \text{ for phase a, b, c}$$

$$\operatorname{Re}(\Delta V_j^n) < \varepsilon; \ j \in \text{ all buses}$$
(12)

$$\operatorname{Im}(\Delta V_j^n) < \varepsilon; \ j \in \text{ all buses}$$

Where ε is the prescribed tolerance. If these equations are satisfied, then the iteration stops. Otherwise, iteration process is repeated. Once the load flow iteration converges all the branch currents and voltage at each bus are known. The real and reactive power loss can therefore be calculated. The flowchart of unbalance power flow using Forward-Backward Propagation is given in Fig. 3.

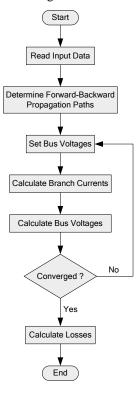


FIGURE 3. THE FLOWCHART FOR THREE-PHASE POWER FLOW CALCULATION USING FORWARD-BACKWARD PROPAGATION ALGORITHM

D. Unbalance Analysis

The system is unbalance if quantities of negative and zero sequence voltages can be observed in the system [1, 12]. Therefore, the level of unbalance may be measured using quantitative unbalance of voltage [9]. This can be calculated using the following equation:

$$MV_{0}(j) = V_{0}(j) / V_{1}(j)$$

$$MV_{2}(j) = V_{2}(j) / V_{1}(j)$$
(13)

Where $MV_0(j)$ and $MV_2(j)$ is the measurement of zeroand positive-sequence voltage with respect to the positive sequence voltage at bus *j*. The sequence component of voltage at bus *j* can be calculated by:

$$\begin{bmatrix} V_{0}(j) \\ V_{1}(j) \\ V_{2}(j) \end{bmatrix} = 1/3^{*} \begin{bmatrix} T \\ V_{b}(j) \\ V_{c}(j) \end{bmatrix}$$
(14)

Where T is transformation matrix for symmetrical components.

IV. SIMULATION

A. System Data

The simulation is carried out for the IEEE 34-bus system [12] indicated in Fig. 4. The system includes balance and unbalance loads. A minor modification has been done for the system to only include three phase asymmetrical lines. However, the load data and the capacitor data are remain the same. The system data and conductors spacing are given in Appendix.

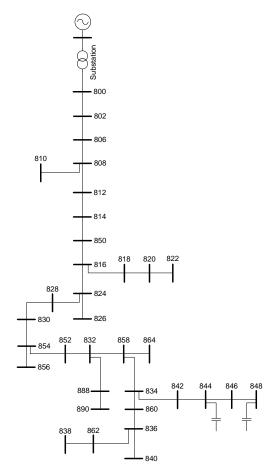


FIGURE 4. THE IEEE 34-BUS SYSTEM USED FOR SIMULATION

B. Simulation Results

The system is run using the algorithm presented in Fig. 3. For the system of Fig. 4, the three-phase power flow calculation takes 5 iterations to converge. This iteration number is fairly small indicating that the algorithm is robust for unbalance power flow calculation. The results of simulation including magnitude and angle of voltage at every phase are given in Table 1. The simulation also indicates the real and reactive power losses of 8.2 kW and 3.4 kVAr, respectively.

bus	Volt a	t phase	Volt at	phase c	Volt at	phase c
no	mag	Angle	mag	Angle	Mag	Angle
800	100	0.00	100	-120.00	100	120.00
802	99.93	-0.01	99.94	-120.01	99.94	119.99
806	99.88	-0.02	99.89	-120.02	99.90	119.98
808	99.01	-0.22	99.19	-120.17	99.17	119.80
810	99.01	-0.22	99.18	-120.18	99.17	119.80
812	97.99	-0.45	98.38	-120.35	98.35	119.58
814	97.18	-0.64	97.75	-120.49	97.70	119.41
816	97.17	-0.64	97.74	-120.49	97.69	119.41
818	97.14	-0.64	97.74	-120.49	97.69	119.41
820	96.32	-0.66	97.84	-120.49	97.66	119.49
822	96.11	-0.67	97.88	-120.49	97.65	119.52
824	97.02	-0.69	97.50	-120.54	97.47	119.33
826	97.02	-0.69	97.49	-120.54	97.48	119.33
828	97.01	-0.69	97.48	-120.54	97.46	119.32
830	96.72	-0.81	97.08	-120.63	97.01	119.17
832	96.20	-1.02	96.36	-120.79	96.19	118.88
834	96.07	-1.08	96.17	-120.84	95.97	118.80
836	96.05	-1.08	96.15	-120.84	95.94	118.80
838	96.04	-1.08	96.14	-120.84	95.94	118.80
840	96.05	-1.08	96.15	-120.84	95.94	118.80
842	96.07	-1.08	96.17	-120.85	95.97	118.80
844	96.07	-1.09	96.16	-120.86	95.96	118.79
846	96.08	-1.11	96.15	-120.87	95.97	118.77
848	96.08	-1.11	96.16	-120.87	95.97	118.77
850	97.18	-0.64	97.75	-120.49	97.70	119.41
852	96.20	-1.02	96.36	-120.79	96.19	118.89
854	96.71	-0.81	97.07	-120.63	97.00	119.16
856	96.71	-0.81	97.06	-120.63	97.00	119.16
858	96.14	-1.05	96.27	-120.82	96.09	118.85
860	96.06	-1.08	96.16	-120.84	95.95	118.80
862	96.05	-1.08	96.15	-120.84	95.94	118.80
864	96.14	-1.05	96.27	-120.82	96.09	118.85
888	96.20	-1.02	96.36	-120.79	96.19	118.89
890	96.18	-1.02	96.34	-120.79	96.17	118.89

TABLE I. SIMULATION RESULTS OF THE IEEE 34-BUS UNBALANCE SYSTEM

The analysis of system unbalance is carried out by measuring the quantitative unbalance of voltage. The ratio of the zero- and negative-sequence voltages with respect to the positive-sequence voltage is calculated using Equation (13) and related results are given in Table 2. It may be observed that the unbalance level of the simulated system is fairly low. This is indicated by small quantities of zero- and negativesequence voltages. Therefore, three-phase power flow enables measuring the unbalance level of the system studied. The unbalance assessment is useful for the purpose of maintaining the system balance level not to exceed the maximum allowable level.

TABLE II. QUANTITATIVE VOLTAGE UNBALANCE OF THE IEEE 34-BUS UNBALANCE SYSTEM

bus no	V0/V1(%)	V2/V1 (%)
800	0	0
802	0.0009	0.0037
806	0.0015	0.0062
808	0.0495	0.0730
810	0.0495	0.0703
812	0.1062	0.1652
814	0.1519	0.2395
816	0.1524	0.2403

818	0.1641	0.2492
820	0.5016	0.5007
822	0.5989	0.5622
824	0.1087	0.2293
826	0.1039	0.2286
828	0.1061	0.2286
830	0.0670	0.2131
832	0.1625	0.1871
834	0.2026	0.1805
836	0.2066	0.1830
838	0.2066	0.1842
840	0.2059	0.1831
842	0.2027	0.1804
844	0.2033	0.1799
846	0.2052	0.1777
848	0.2051	0.1776
850	0.1519	0.2396
852	0.1625	0.1871
854	0.0670	0.2127
856	0.0626	0.2120
858	0.1806	0.1843
860	0.2088	0.1805
862	0.2066	0.1831
864	0.1806	0.1844
888	0.1625	0.1871
890	0.1623	0.1870

V. CONCLUSION

Three-phase power flow for an unbalance distribution system is carried out using Forward-Backward Propagation Technique. The IEEE 34-bus unbalance system is used for simulation. The main conclusions are:

- The implemented algorithm works directly on the simulated system and, therefore, there is no need to transform the system into the symmetrical components as well as to decouple the three-phase into individual phases;
- The algorithm is robust for the radial unbalance distribution system with good convergence characteristic;
- The unbalance level of three-phase system may only be assessed by performing three-phase power instead of single-phase (balance) power flow.

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BIOGRAPHY

Agus Ulinuha received the B.S. degree in 1994 from Universitas Diponegoro, Semarang, Indonesia, M.S. degree in 1999 from Universitas Gadjah Mada, Indonesia, and PhD degree from Curtin University of Technology, Australia in 2007. His research interest includes optimization of electrical system and harmonics.

APPENDIX

TABLE A. SHUNT CAPACITOR OF IEEE 34-BUS SYSTEM

Bus#	Connection	Phase A (kVAr)	Phase B (kVAr)	Phase C (kVAr)
844	Y	100	100	100
848	Y-grd	150	150	150

TABLE B. BALANCE LOADS OF IEEE 34-BUS SYSTEM

Bus		Phas	se A	Phas	se B	Pha	se C
#		kW	kVAr	kW	kVAr	kW	kVAr
860		19.91	15.94	19.91	15.94	19.91	15.94
840		8.86	7.09	8.86	7.09	8.86	7.09
844		133.444	106.83	133.444	106.88	133.444	106.88
848		19.45	15.57	19.45	15.57	19.45	15.57
890		27	21.62	27	21.62	27	21.62

TABLE C. UNBALANCE LOADS OF IEEE 34-BUS SYSTEM

Bus	Phase A		Phase B		Phase C	
#	kW	kVAr	kW	kVAr	kW	kVAr
806	0	0	31.22	16.14	26.07	13.84
810	0	0	15.88	8.21	0	0
820	33.9	17.52	0	0	0	0
822	135.5	70.07	0	0	0	0
824	0	0	0.39	0.2	0	0
826	0	0	41.93	21.68	0	0
828	0	0	0	0	2.78	1.44
830	6.18	3.2	0	0	0	0
834	3.99	2.06	12.55	6.49	12.82	6.63
836	27.37	14.15	10.55	5.45	42.05	21.74
838	27.61	14.27	0	0	0	0
840	17.49	9.04	21.81	11.27	0	0
842	0	0	0	0	0	0
844	9.12	4.71	0	0	0	0
846	0	0	24.59	12.71	22.23	11.49
848	0	0	22.62	11.7	0	0
856	0	0	3.71	1.92	0	0
858	6.68	3.45	1.08	0.56	5.35	2.77
860	15.66	8.09	20.86	10.78	111.15	57.46
862	0	0	0	0	0	0
864	0.63	0.33	0	0	0	0

Swing : bus 800; MVA base: 2.5 MVA

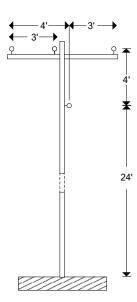


FIGURE A. OVERHEAD LINE SPACING OF IEEE 34-BUS SYSTEM

Bus		Configuration	length	Line Co	Line Conductor		Neutral Conductor	
From	То	Comiguration	(ft)	$R(\Omega/mi)$	GMR (ft)	$R(\Omega/mi)$	GMR (ft)	
800	802	BACN	2580	1.69	0.00418	1.69	0.00418	
802	806	BACN	1730	1.69	0.00418	1.69	0.00418	
806	808	BACN	32230	1.69	0.00418	1.69	0.00418	
808	810	BCAN	5840	2.55	0.00452	2.55	0.00452	
808	812	BACN	37500	1.69	0.00418	1.69	0.00418	
812	814	BACN	29730	1.69	0.00418	1.69	0.00418	
814	850	BACN	10	1.69	0.00418	1.69	0.00418	
816	818	ABCN	1710	2.55	0.00452	2.55	0.00452	
816	824	BACN	10210	1.69	0.00418	1.69	0.00418	
818	820	ABCN	48150	2.55	0.00452	2.55	0.00452	
820	822	ABCN	13740	2.55	0.00452	2.55	0.00452	
824	826	BCAN	3030	2.55	0.00452	2.55	0.00452	
824	828	BACN	840	1.69	0.00418	1.69	0.00418	
828	830	BACN	20440	1.69	0.00418	1.69	0.00418	
830	854	BACN	520	1.69	0.00418	1.69	0.00418	
832	858	BACN	4900	1.69	0.00418	1.69	0.00418	
832	888	BACN	100	1.69	0.00418	1.69	0.00418	
834	860	BACN	2020	1.69	0.00418	1.69	0.00418	
834	842	BACN	280	1.69	0.00418	1.69	0.00418	
836	840	BACN	860	1.69	0.00418	1.69	0.00418	
836	862	BACN	280	1.69	0.00418	1.69	0.00418	
842	844	BACN	1350	1.69	0.00418	1.69	0.00418	
844	846	BACN	3640	1.69	0.00418	1.69	0.00418	
846	848	BACN	530	1.69	0.00418	1.69	0.00418	
850	816	BACN	310	1.69	0.00418	1.69	0.00418	
852	832	BACN	10	1.69	0.00418	1.69	0.00418	
854	856	BCAN	23330	2.55	0.00452	2.55	0.00452	
854	852	BACN	36830	1.69	0.00418	1.69	0.00418	
858	864	ABCN	1620	2.55	0.00452	2.55	0.00452	
858	834	BACN	5830	1.69	0.00418	1.69	0.00418	
860	836	BACN	2680	1.69	0.00418	1.69	0.00418	
862	838	ACBN	4860	1.69	0.00418	1.69	0.00418	
888	890	BACN	10560	1.12	0.00446	1.12	0.00446	

TABLE D. BRANCH DATA OF IEEE 34-BUS SYSTEM