

Bab. VI : Lampiran

Untuk mencari Rumus Slow Moving, Semi Fast Moving dan Fast Moving. didalam "Inventory Control" dengan metoda multiplikasi Lagrange adalah sebagai berikut.

I. Slow moving

$St = 2 \times$ (banyak barang per pesanan) - (kebutuhan per bulan).

$$St = 2 X_i - \frac{Z_i}{12}$$

$$n = \frac{12}{N} \text{ dimana } N = \frac{Z_i}{X_i}$$

$$n = \frac{12 X_i}{Z_i}$$

$$T.C = C_r \sum \frac{Z_i}{X_i} + C_t \sum \frac{X_i C_i}{2} + C_s \sum [X_i + St - (n-1)(\text{kebutuhan pra bulan})] C_i$$

$$T.C = 750 \sum \frac{Z_i}{X_i} + 0,12 \sum \frac{X_i C_i}{2} + 0,10 \sum [X_i + (2X_i - \frac{Z_i}{12}) - (\frac{12X_i}{Z_i} - 1)(\frac{Z_i}{12})] C_i$$

$$T.C = 750 \sum \frac{Z_i}{X_i} + 0,26 \sum X_i C_i.$$

Pembatas

a). Alokasi dana $\leq \sum \frac{Z_i C_i}{4}$

$$g1 \equiv X_i C_i - 0,25 Z_i C_i = 0$$

b). Kapasitas penyimpanan barang didalam gudang TAK ADA.

$$g2 \equiv 0$$

c). Jumlah bunga maximal yang harus dikembalikan $\leq 20\% \sum \frac{Z_i C_i}{4}$

$$g3 \equiv \sum [X_i + St - (n-1)(\text{kebutuhan pra bulan})(1+t)^{n-1}] - 20\% \sum \frac{Z_i C_i}{4}$$
$$\equiv \sum [X_i + 2X_i - \frac{Z_i}{12} - (\frac{12X_i}{Z_i} - 1)(\frac{Z_i}{12}) \{ (1,015)^3 + (1,015)^2 + (1,015) + 1 \}] - 0,05 \sum Z_i C_i$$

$$\equiv -1,0909 \sum X_i + 0,2578 \sum Z_i - 0,05 \sum Z_i C_i = 0$$

Persamaan Lagrange

$$\begin{aligned} R &= T.C + \lambda (g_1 + g_2 + g_3) \\ &= 750 \sum \frac{z_i}{x_i} + 0,26 \sum x_i c_i + \lambda \left[\sum x_i c_i - 0,25 \sum z_i c_i \right. \\ &\quad \left. - 1,0909 \sum x_i + 0,25758 \sum z_i - 0,05 \sum z_i c_i \right] \end{aligned}$$

$$\frac{\partial R}{\partial x_i} = -\frac{750 z_i}{x_i^2} + 0,26 c_i + \lambda (c_i - 1,0909)$$

$$\frac{\partial R}{\partial \lambda} = \sum x_i c_i - 0,3 \sum z_i c_i - 1,0909 \sum x_i + 0,25758 \sum z_i$$

$$\begin{aligned} \therefore \frac{\partial R}{\partial x_i} &= 0 \\ \frac{\partial R}{\partial \lambda} &= 0 \end{aligned}$$

maka $-\frac{750 z_i}{x_i^2} + 0,26 c_i + \lambda (c_i - 1,0909) = 0.$

$$x_i^2 = \frac{750 z_i}{0,26 c_i + \lambda (c_i - 1,0909)}$$

$$x_i = \sqrt{\frac{750 z_i}{0,26 c_i + \lambda (c_i - 1,0909)}}$$

$$\sum x_i (c_i - 1,0909) = 0,3 \sum z_i c_i - 0,25758 \sum z_i$$

$$\frac{750 z_i (c_i - 1,0909)^2}{0,26 c_i + \lambda (c_i - 1,0909)} = (0,3 \sum z_i c_i - 0,25758 \sum z_i)^2$$

$$\lambda = \frac{750 (c_i - 1,0909)}{(0,3 \sum c_i - 0,25758)^2} - \frac{0,26 c_i}{(c_i - 1,0909)}$$

II. Semi Fast moving dan Fast moving.

$$S_t = 2 \times (\text{banyak barang pra pesanan}) - (\text{lead time}) (\text{kebutuhan pra bulan})$$

$$S_t = 2 X_i - \frac{Z_i}{24}$$

$$n = \frac{12X_i}{Z_i}$$

$$\begin{aligned} T.C &= C_r \sum \frac{Z_i}{X_i} + C_t \sum \frac{X_i C_i}{2} + C_s \sum \left[X_i + S_t - (n-1)(\text{kebutuhan pra bulan}) \right] C_i \\ &+ C_r \sum \left[X_i + S_t - (n-1)(\text{kebutuhan pra bulan}) \right] C_i \\ &= 750 \sum \frac{Z_i}{X_i} + 0,12 \sum \frac{X_i C_i}{2} + 0,10 \sum \left[X_i + 2X_i - \frac{Z_i}{24} - \left(\frac{12X_i}{Z_i} - 1 \right) \left(\frac{Z_i}{12} \right) \right] C_i \\ &+ 0,15 \sum \left[X_i + 2X_i - \frac{Z_i}{24} - \left(\frac{12X_i}{Z_i} - 1 \right) \left(\frac{Z_i}{12} \right) \right] C_i \end{aligned}$$

$$T.C = 750 \sum \frac{Z_i}{X_i} + 0,56 \sum X_i C_i + 0,0104 \sum Z_i C_i.$$

Pembatas

a). Alokasi dana $\leq \sum \frac{Z_i C_i}{4}$

$$g_1 = \sum X_i C_i - \sum \frac{Z_i C_i}{4}$$

b). Kapasitas penyimpanan barang didalam gudang ≤ 10.000 unit.

$$g_2 = \sum 2 \times \left[\text{jumlah pesanan pra order} - \text{lead time (kebutuhan pra bulan)} \right] - 10.000.$$

$$g_2 = \sum 2 \left[X_i - \frac{1}{2} \left(\frac{Z_i}{12} \right) \right] - 10.000.$$

$$g_2 = 2 \sum X_i - 0,08333 \sum Z_i - 10.000.$$

c). Jumlah bunga maximal yang harus dikembalikan $20\% \leq \sum \frac{Z_i C_i}{4}$

$$g_3 = \sum \left[X_i + S_t - (n-1)(\text{kebutuhan pra bulan}) \right] (1+t)^{n-1} - 0,05 \sum Z_i C_i.$$

$$g_3 = 0,2991 \sum Z_i - 1,0909 \sum X_i - 0,05 \sum Z_i C_i.$$